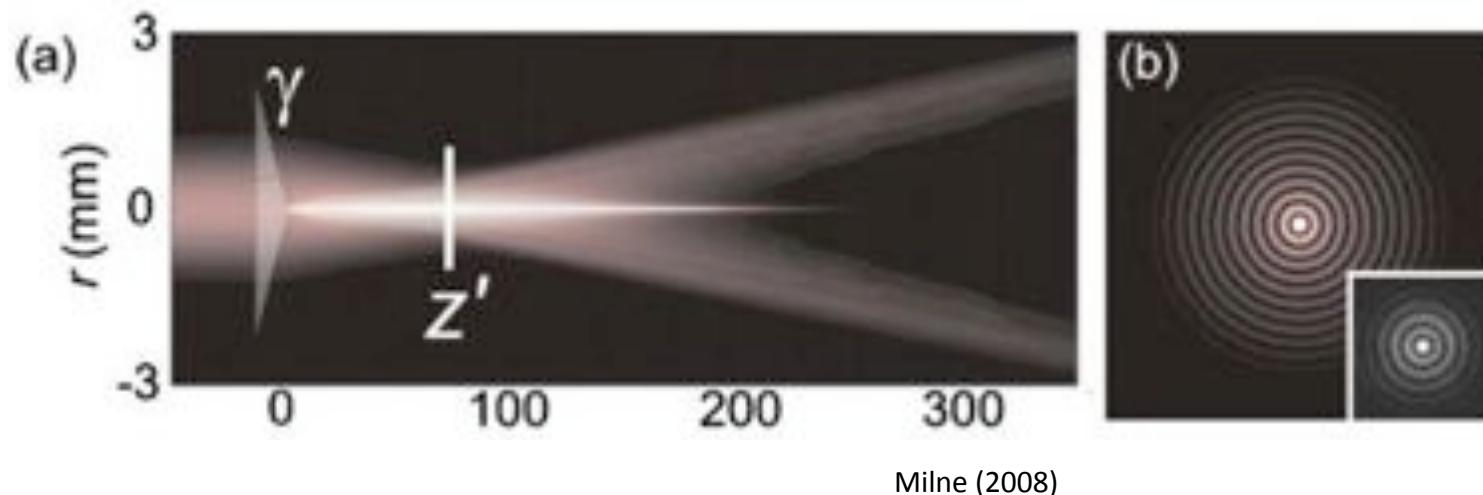


Creating Bessel Beams



Melia Bonomo, Dickinson College
Marissa Romano, Stony Brook University



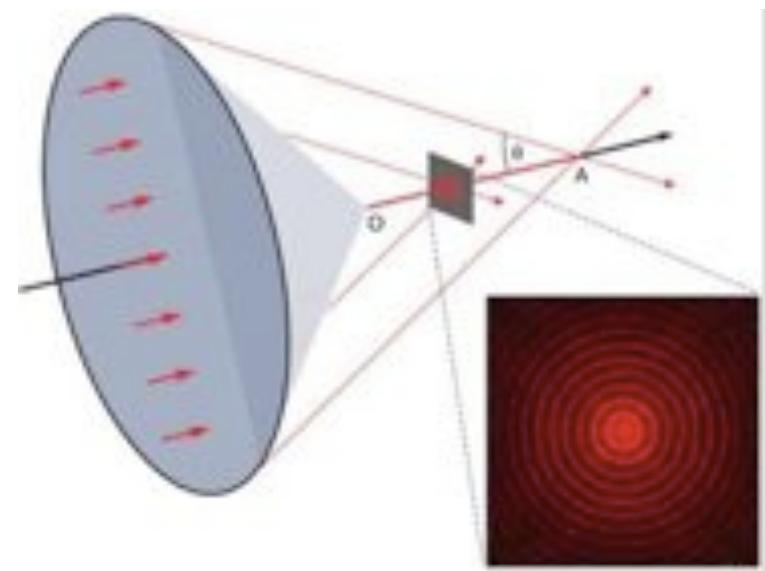
Laser Teaching Center
Summer 2012
Stony Brook University



Welcome to the Laser Center

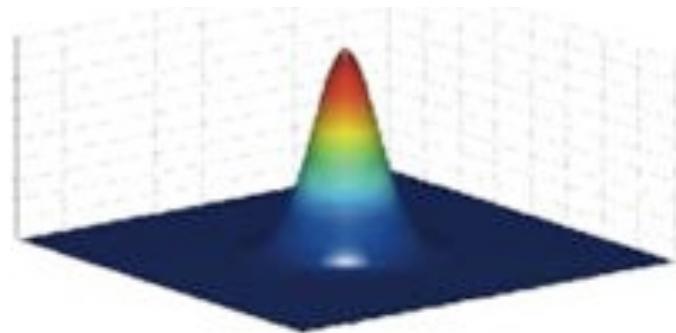
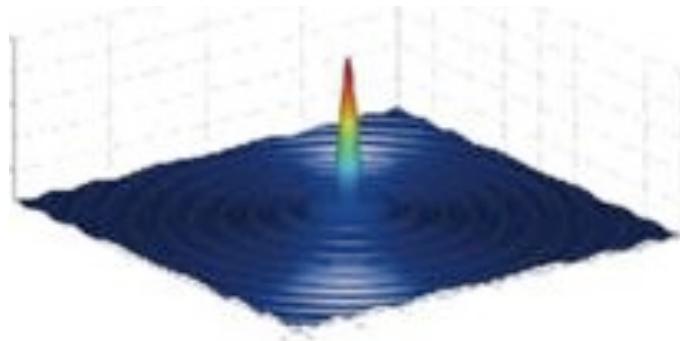
Overview

- Bessel beam properties
- Generating Bessel beams
 - Annular Aperture
 - 4-f Spatial Filtering
 - Axicon
 - TAG Lens

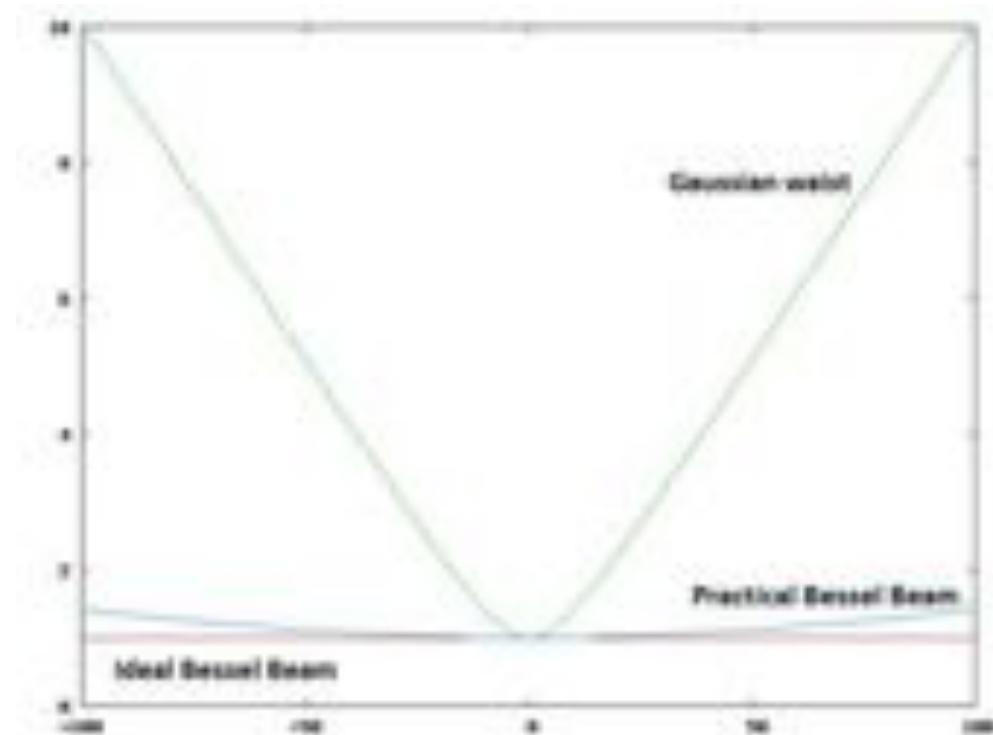


Jaroszewicz (2005)

Bessel vs. Gaussian Beams

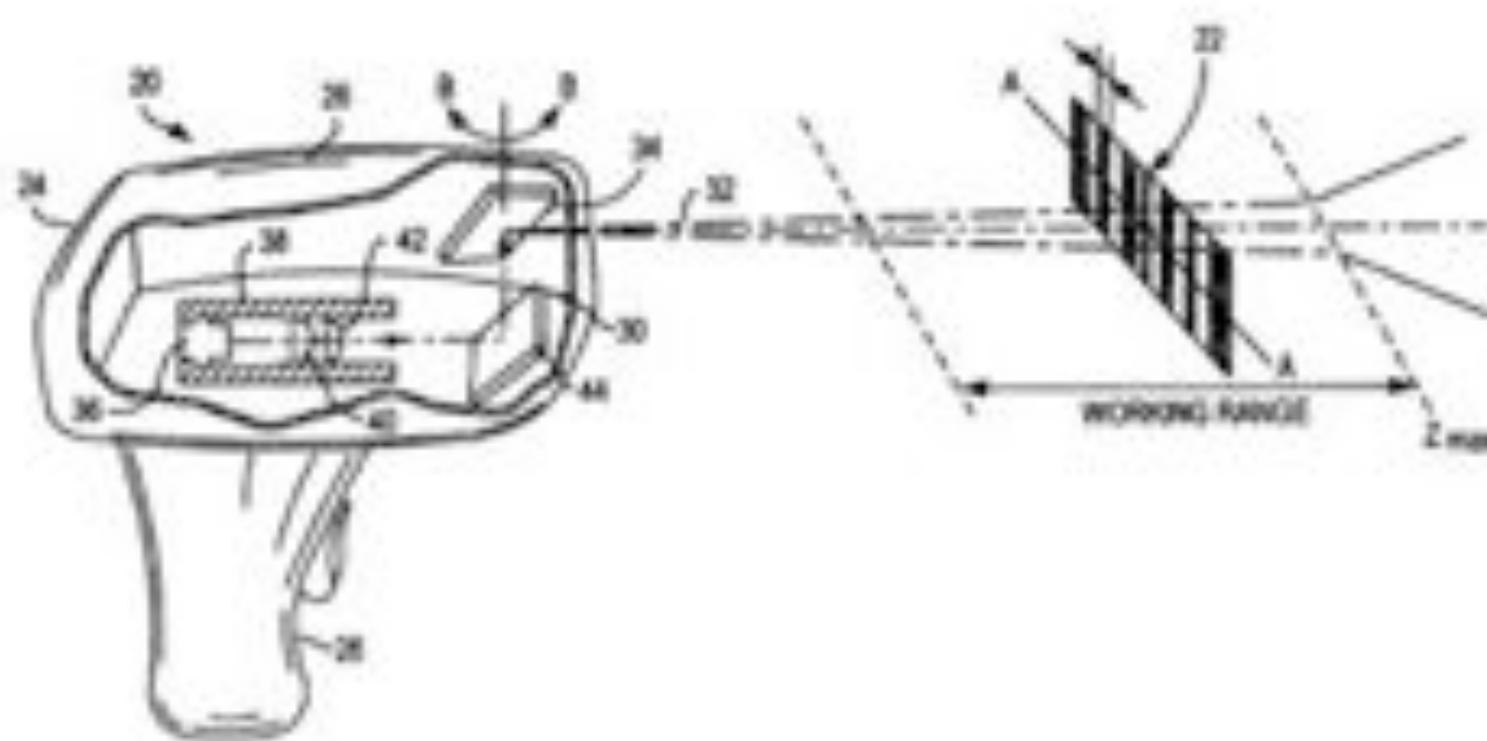


- Non-diffracting
- Thin, infinitely long core with concentric rings
- Ideal Bessel beams cannot be experimentally created
- Close approximations are possible



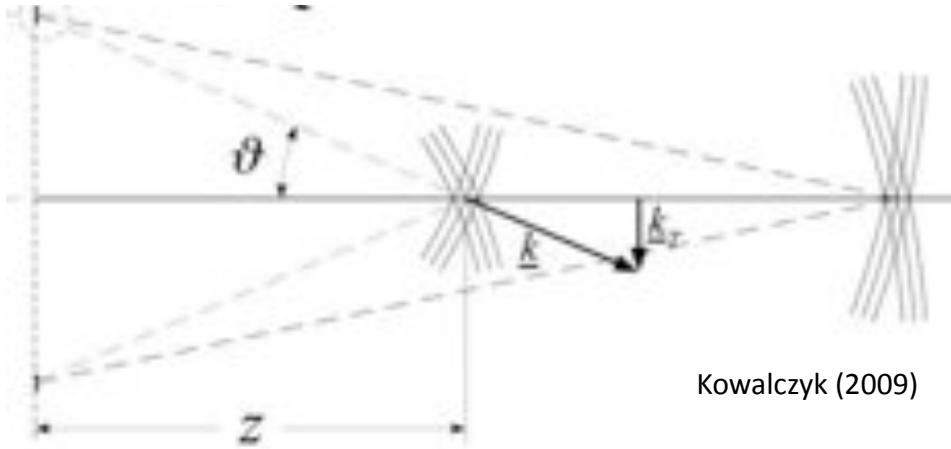
Most Widespread Application

- Employing a Bessel beam greatly increases the working range of a barcode scanner



Gurevich 2003

Geometry and Math

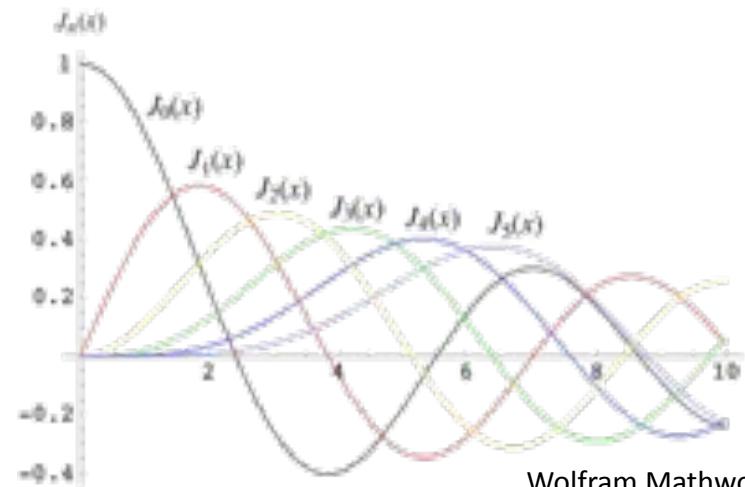


Kowalczyk (2009)

- Superposition of plane waves with \mathbf{k} -vectors lying on surface of cone
 - Creates central max and plurality of side lobes

$$E_l(r, \phi, z) = A e^{i k_z z} J_l(k_r r) e^{i \phi l}$$

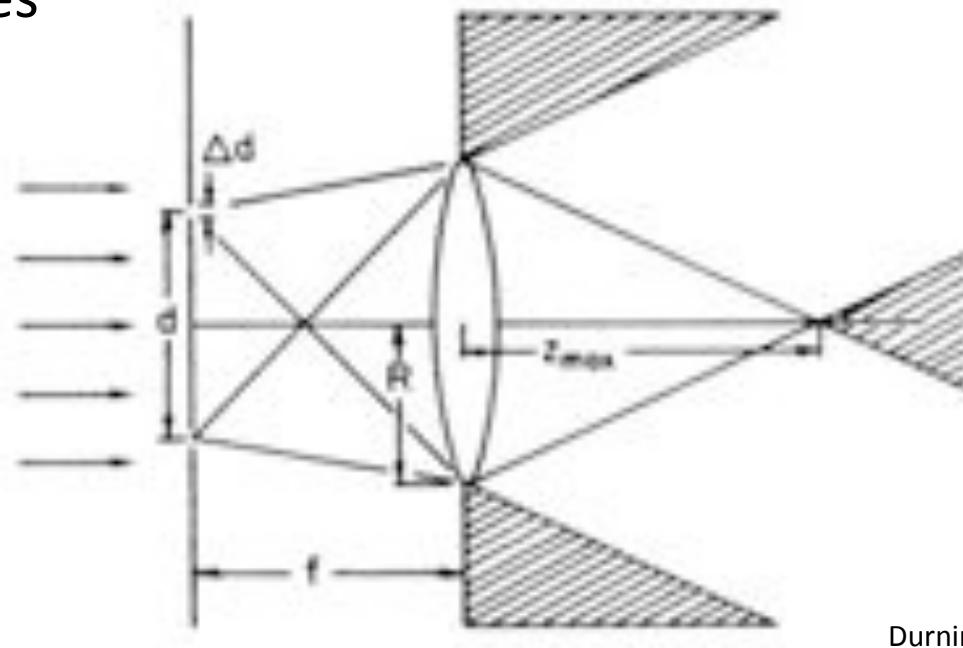
- Electric field amplitude proportional to Bessel function



Wolfram Mathworld, 2012

Creating Bessel beams with an Annular Aperture

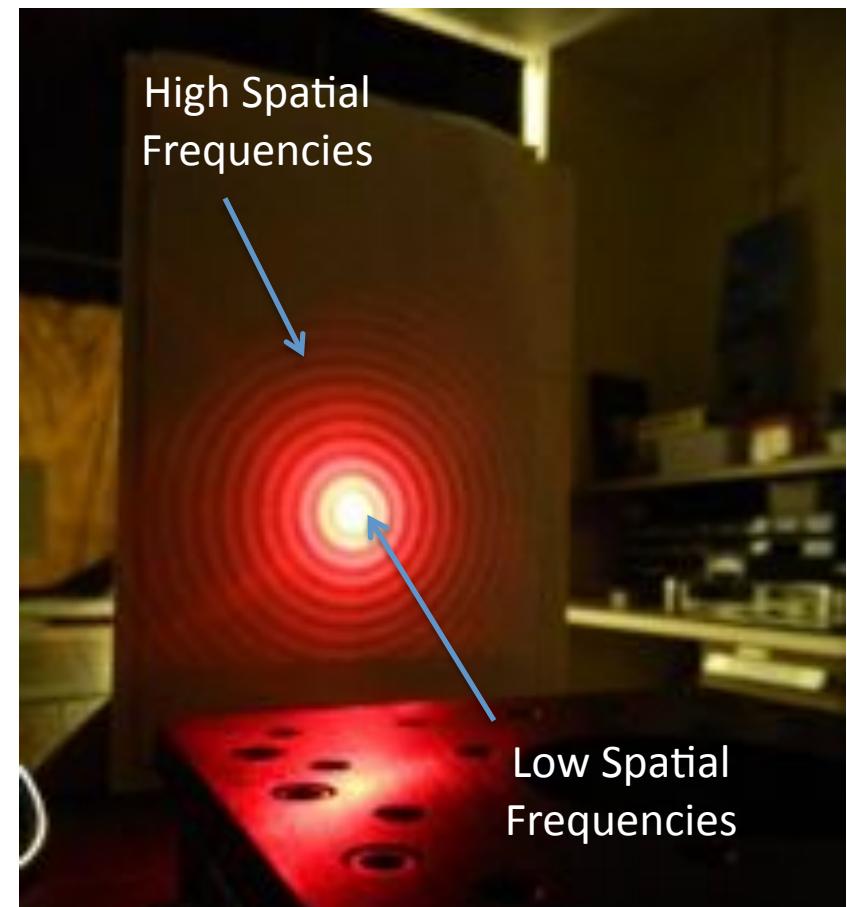
- Fresnel diffraction of thin ring light source
- Durnin and Eberly 1987
 - 2.5 mm diameter, 10 micron wide
- Lens collimates ring of light to create conical superposition of plane waves



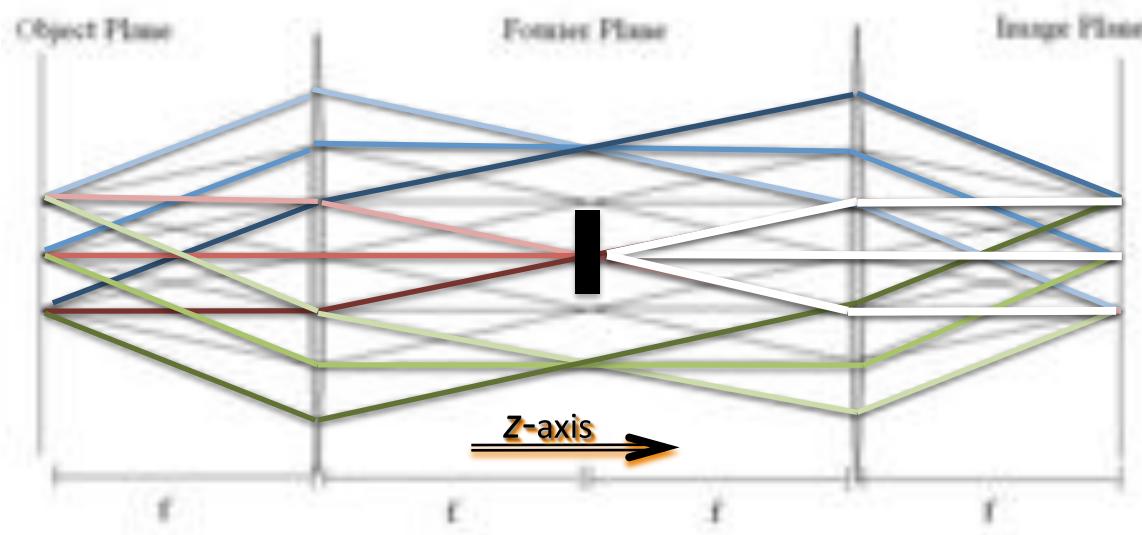
Durnin and Eberly (1987)

Creating a ring of light through spatial filtering a circular aperture

- Pinhole diffraction pattern in Fourier plane
 - High spatial frequencies: object edges
 - Low spatial frequencies: overall quality
- Edge-enhanced image of the circular aperture



4-f Spatial Filtering Method

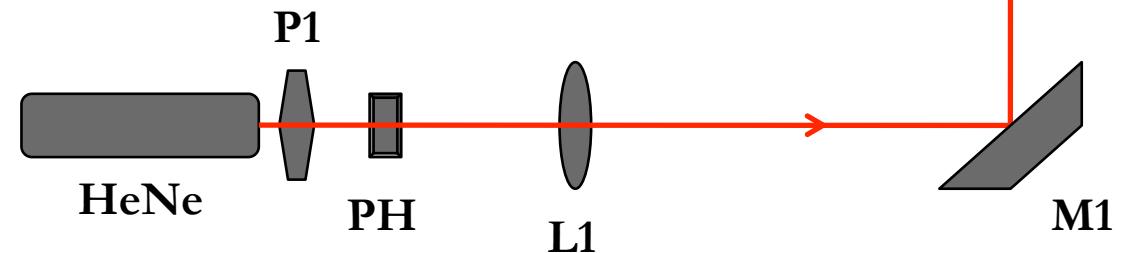
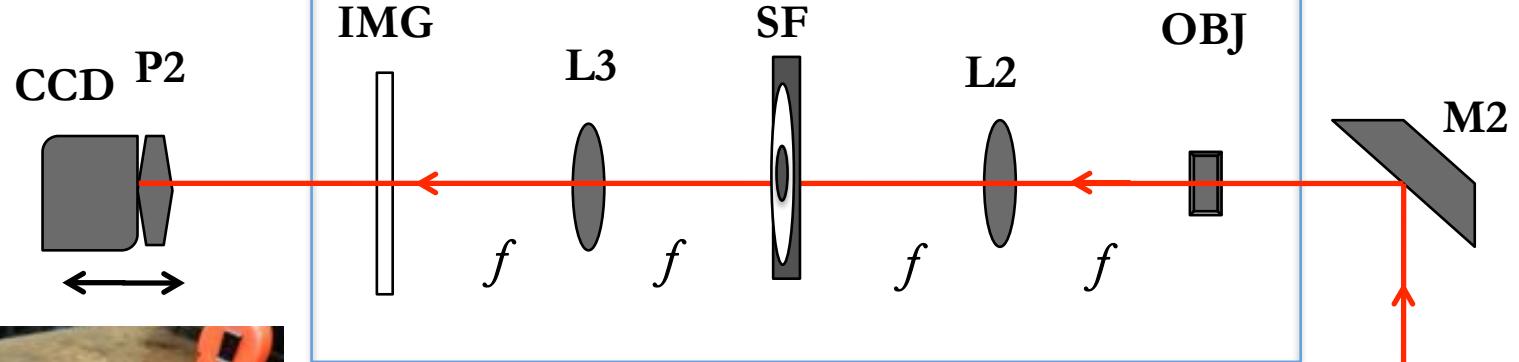


- Lens organizes spatial frequencies of object
 - Rays bent at same angle are part of the same diffraction order of the pattern in the Fourier plane
- The diffraction pattern is the Fourier transform of the object
- Inverse image created in image plane



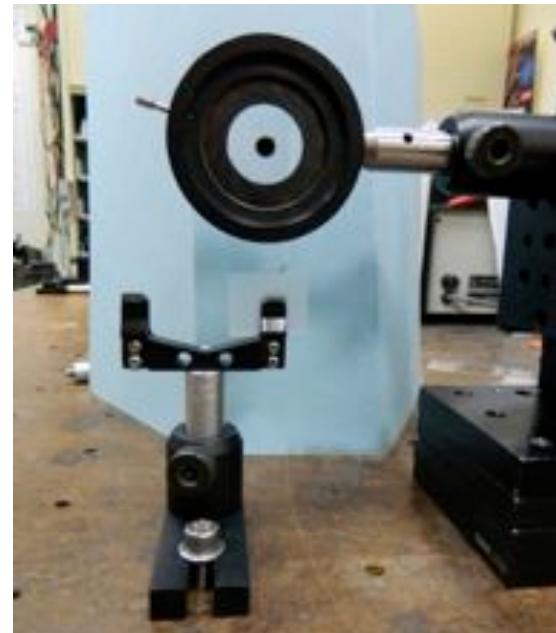
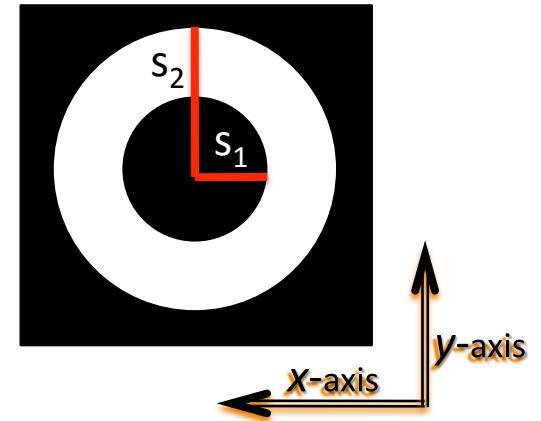
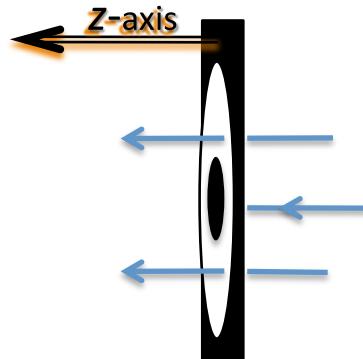
Setup Design

Z-axis



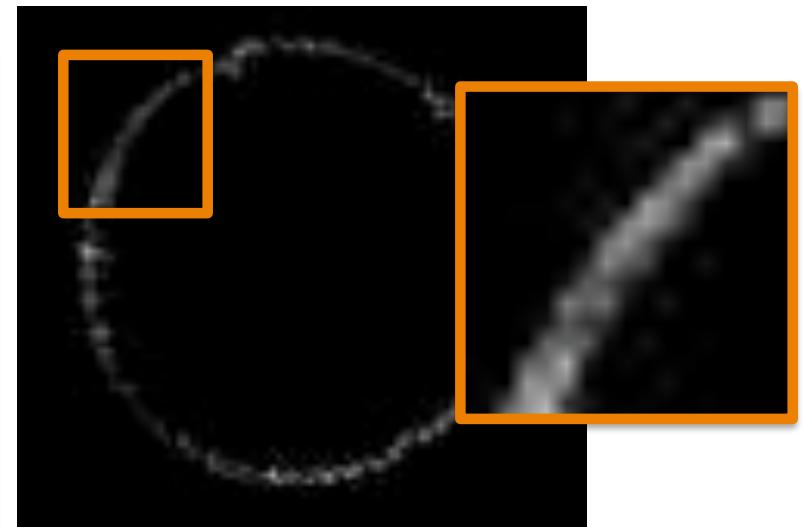
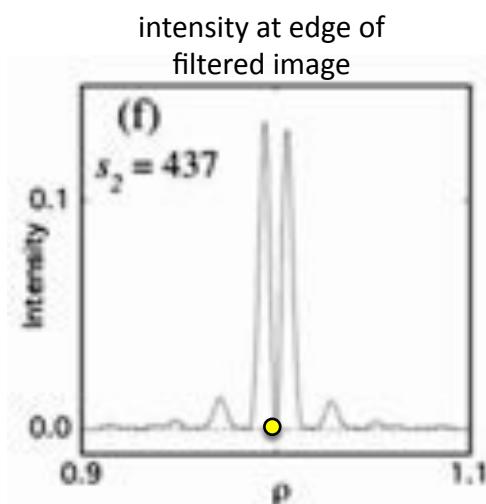
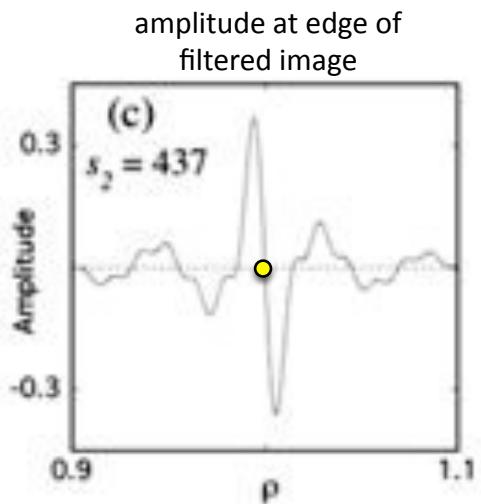
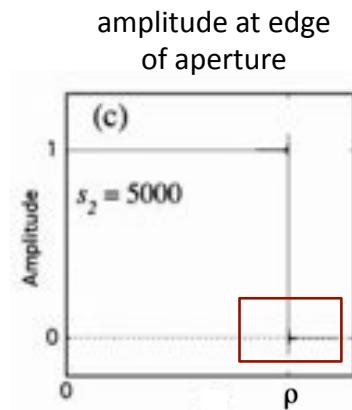
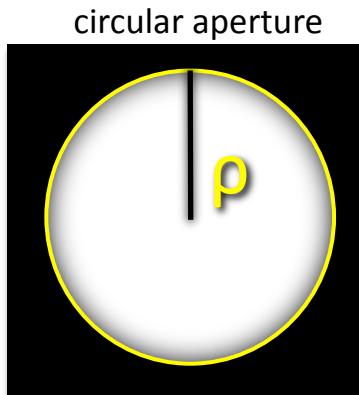
The filter dimensions

- Inner radius 3 mm
 - To block the low frequencies
- Outer iris diaphragm radius 10 mm
 - Limits the high frequencies coming through too
- Why is there a limit on the outer dimension?



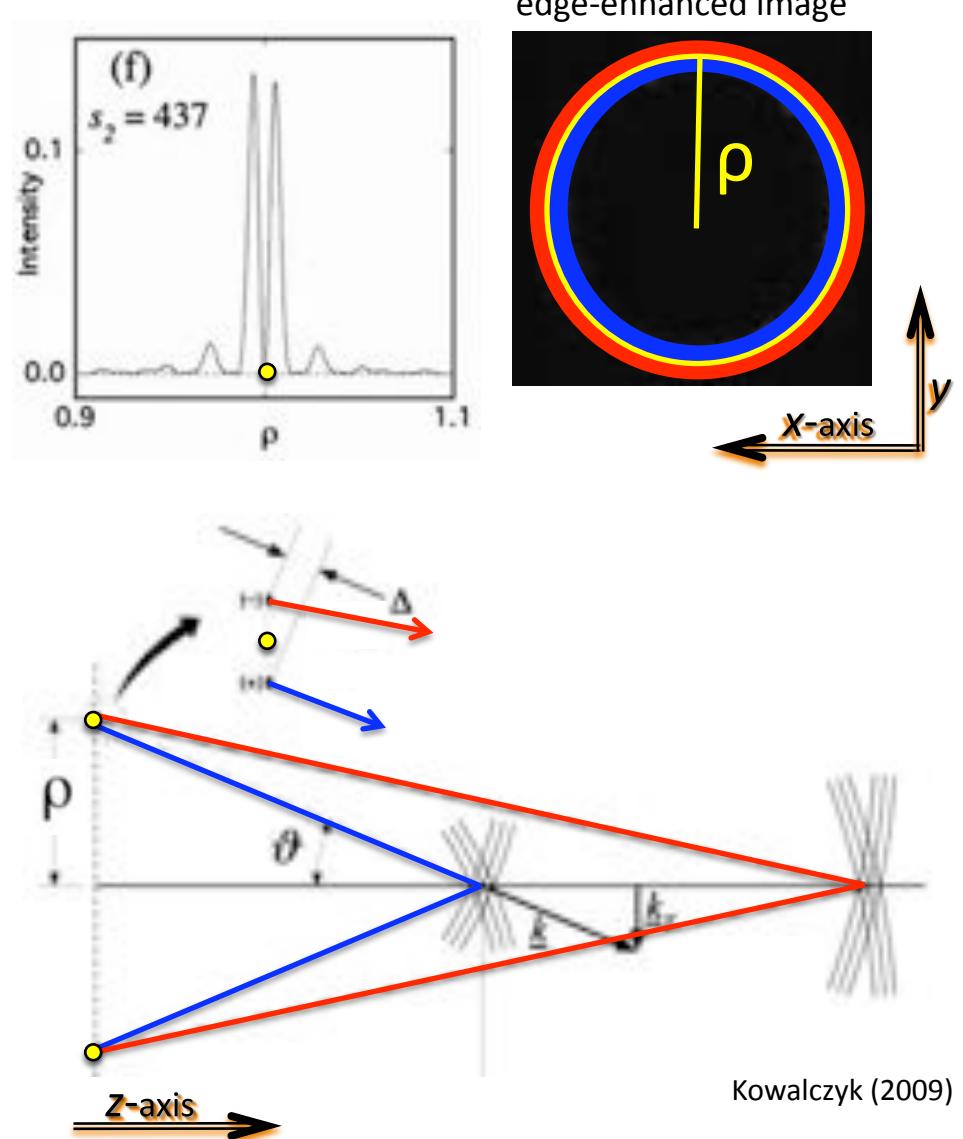
Gibb's phenomenon

- Always a zero in the middle of the diffracted field at $r = \rho$
- Causes double-lobed amplitude at edge of aperture
- This is the difference between our ring and that which would have come from a uniformly illuminated annular slit



Forming the Bessel beam

- Propagation delay Δ between double-lobed intensity
- As you go farther on z-axis the lobes spread apart
 - constructive interference
 - start of Bessel beam
- Until a certain point where the lobes are too spread
 - destructive interference
 - end of the Bessel beam



Kowalczyk (2009)



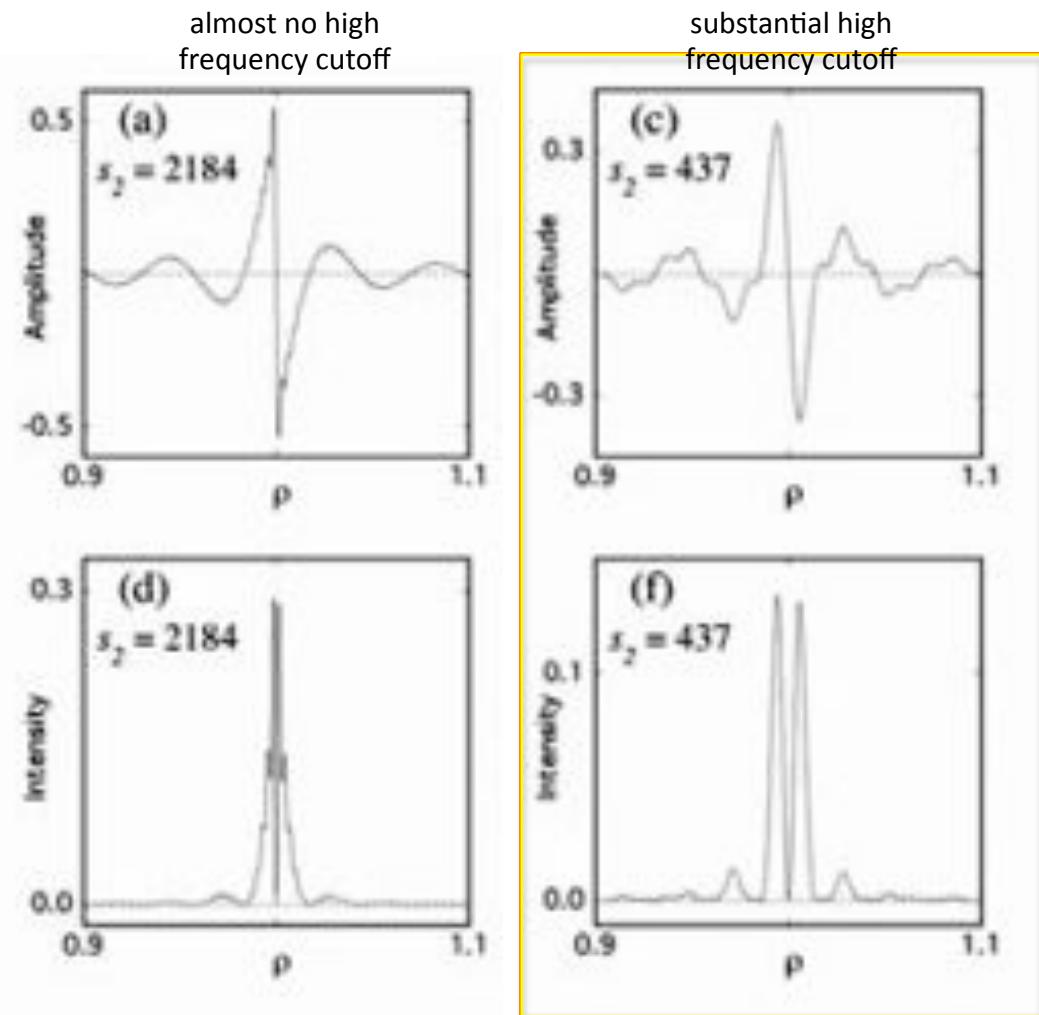
Technically speaking

- “Bessel beam” normally used to describe non-diverging beams
- Here, we’re making use of a diverging pattern to create the Bessel-like beam
- Still has a Bessel function radial profile and exhibits the characteristic properties



Effect of outer frequency cutoff on separation between intensity lobes

- Cutting off high frequencies:
 - less of an overshoot
 - lobes are more distinguishable from each other
 - larger propagation delay between lobes
 - larger region of constructive interference on axis
 - longer Bessel beam



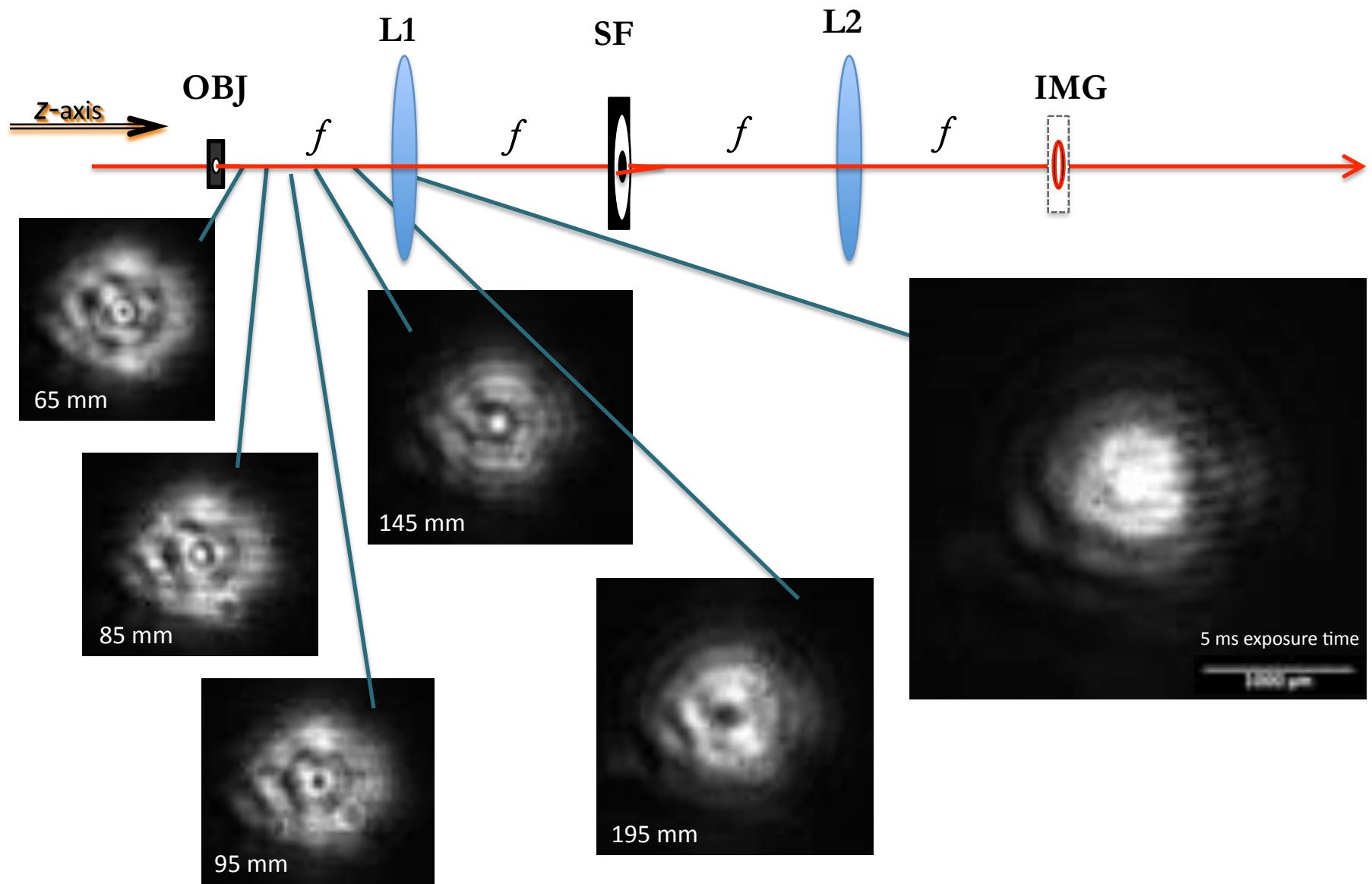
Kowalczyk (2009)

Electrim EDC 1000N images

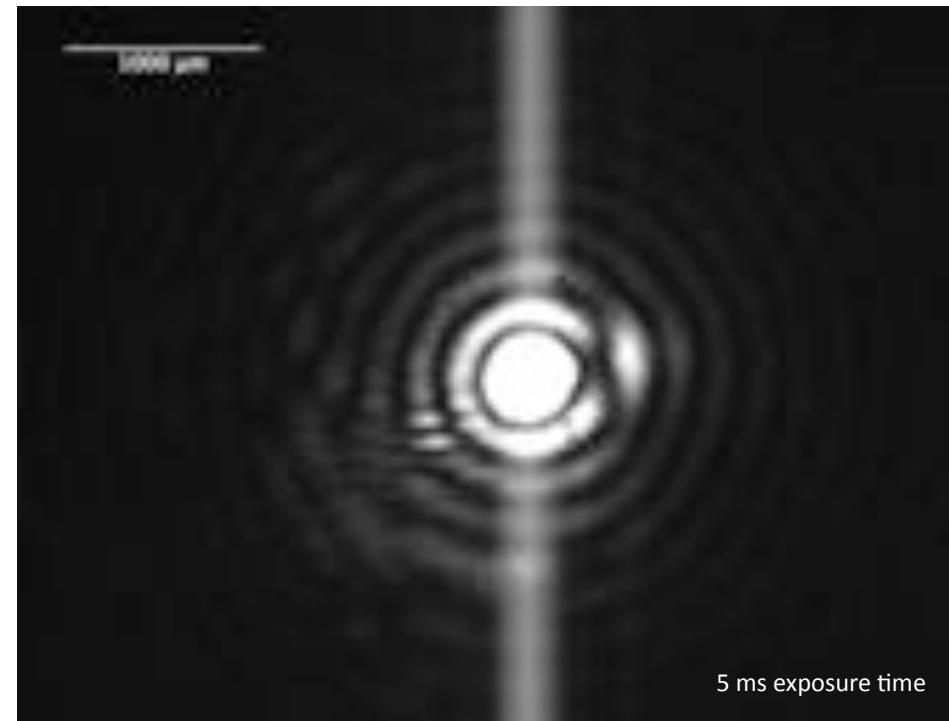
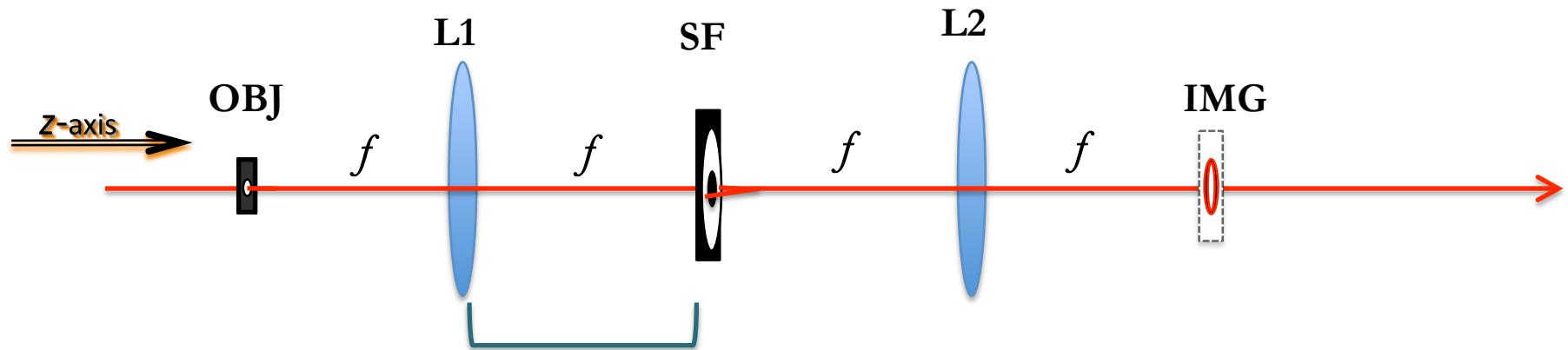
- 7.4 micron square pixels
- Polarizers to prevent saturation
- Recorded the evolution of the light field from the initial aperture to the final Bessel beam
- Images are transverse taken in transverse plane



Object to Lens 1

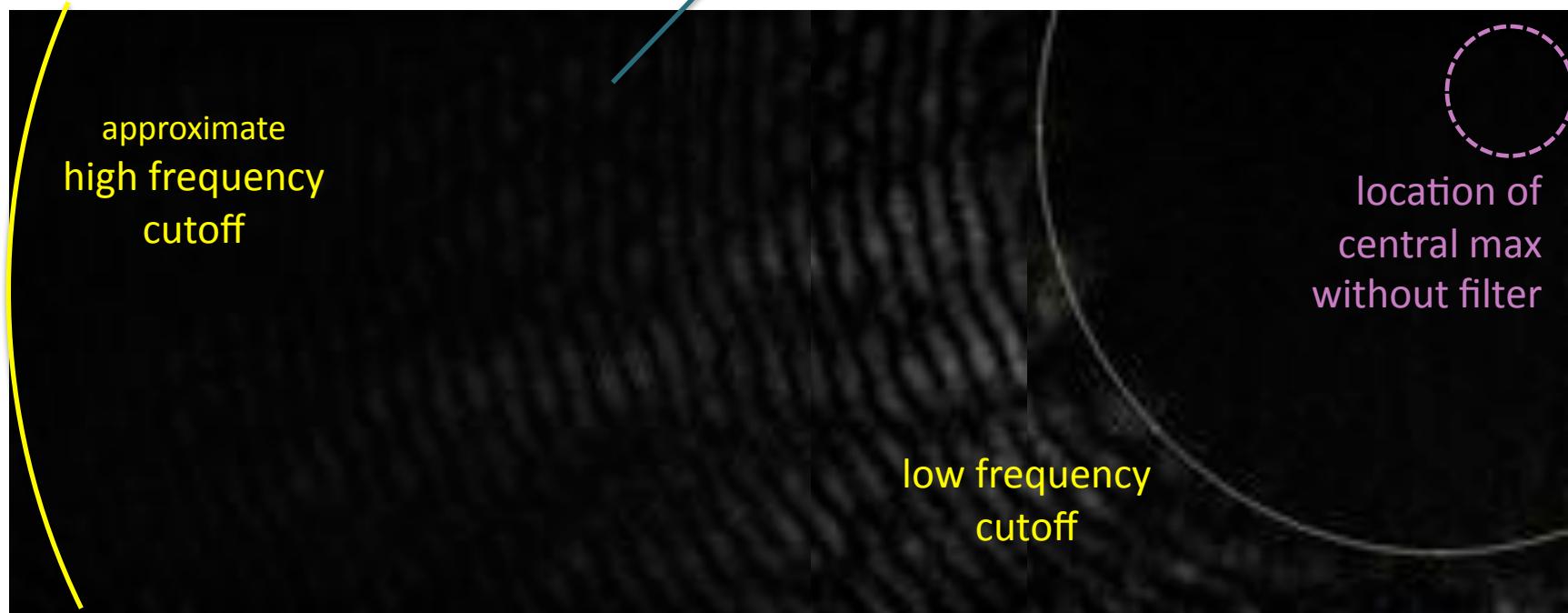
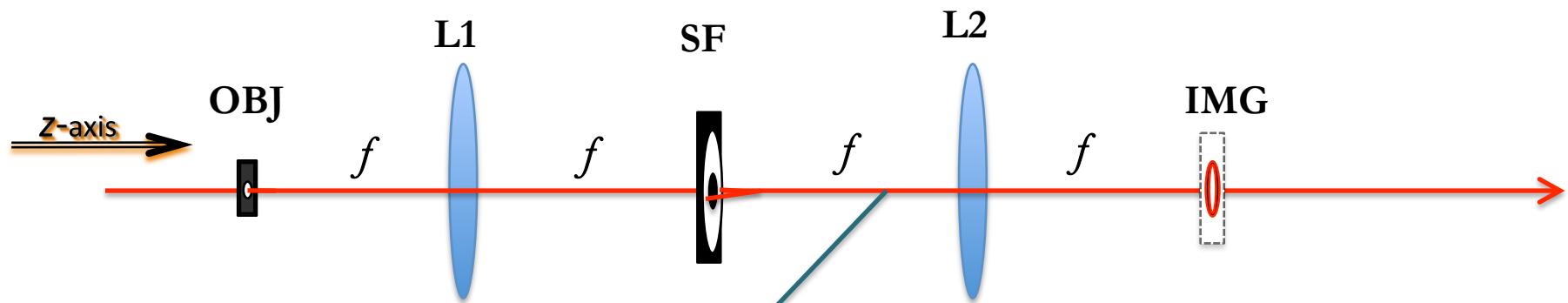


Lens 1 to Spatial Filter



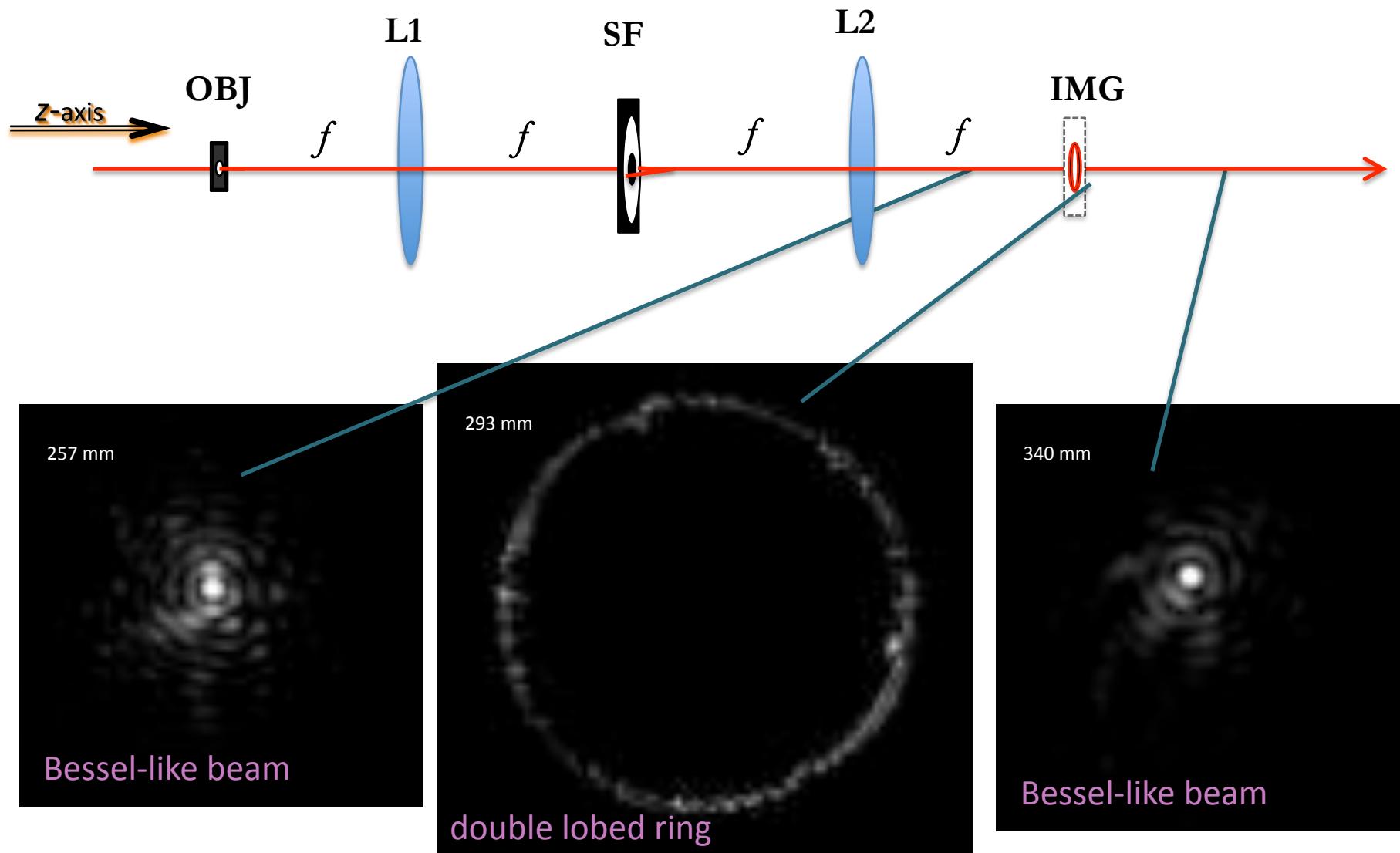
classic Airy
pattern

Spatial Filter to Lens 2



190 mm from Fourier plane

Lens 2 to Image Plane and Beyond



The formation of the Bessel beam



- First starts at about 220 mm from the final lens
- Propagates 47 mm
- Disappears 267 mm

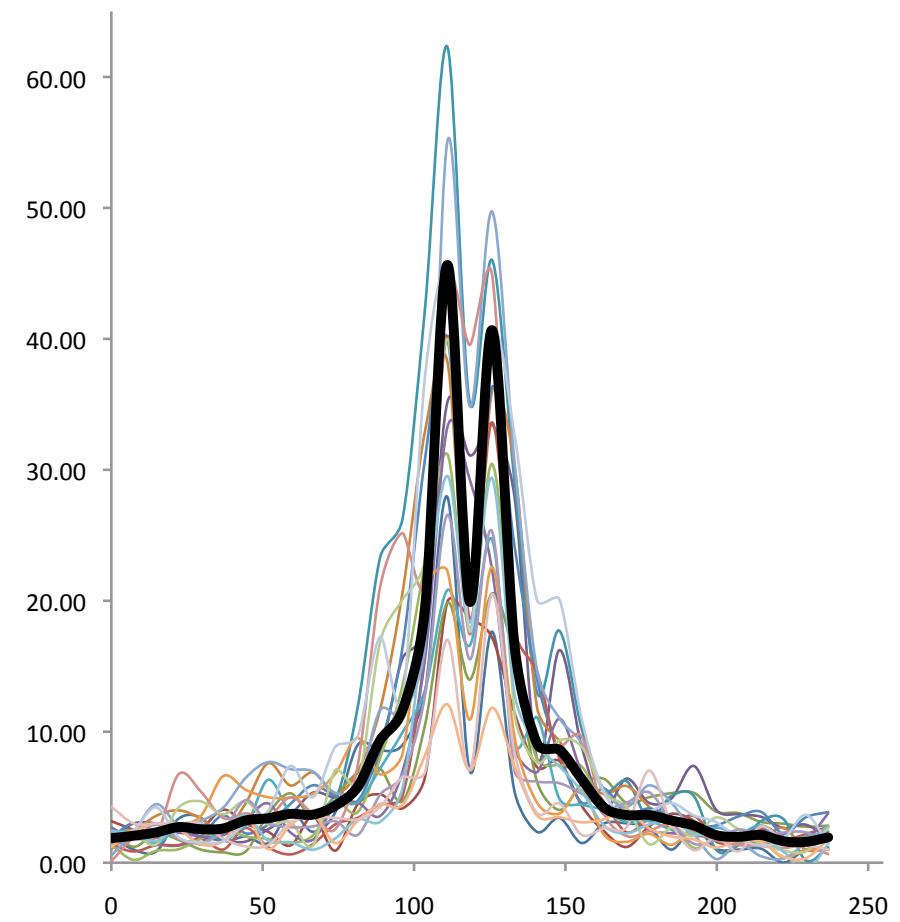
- Ring of light comes to focus at 293 mm

- Bessel beam appears again at 320 mm
- 47 mm propagation
- 376 mm it disappears

ImageJ Analysis: thin ring of light



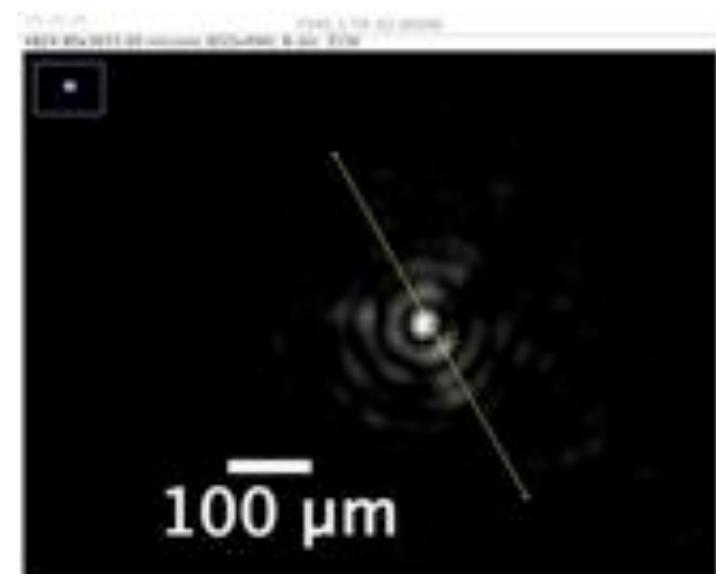
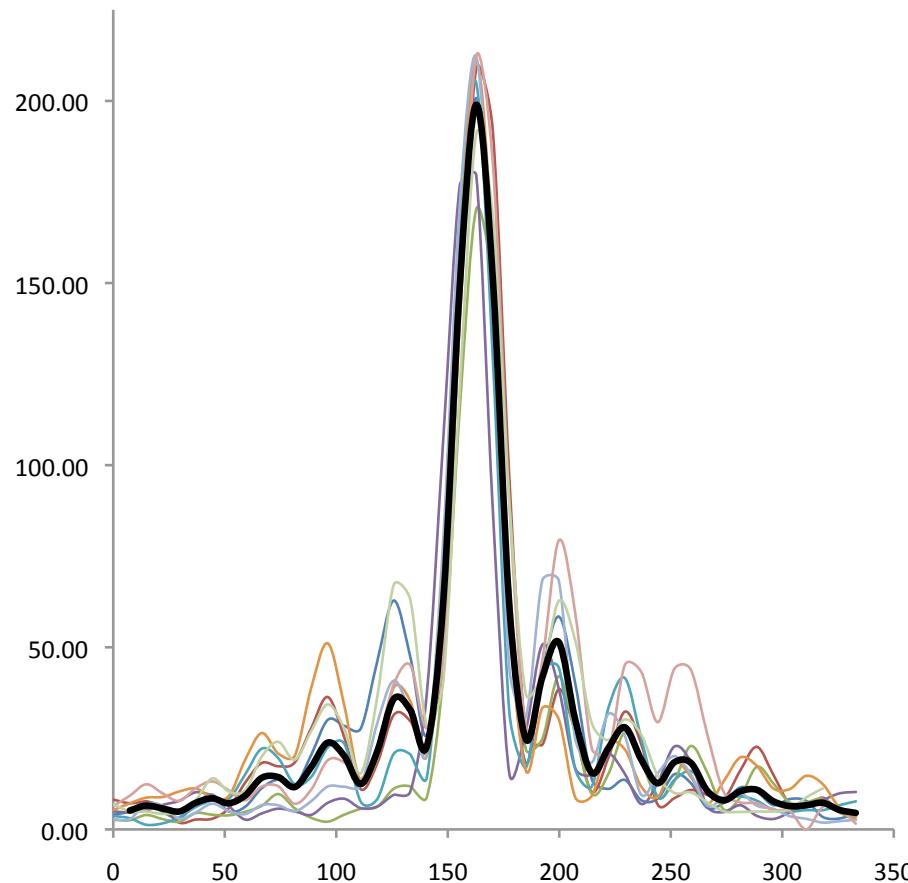
- Average radial intensity profile of double-lobed ring source at focal point
- Spacing between lobes about $14.8 \mu\text{m}$



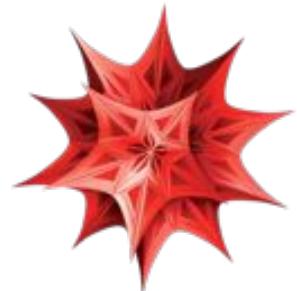
ImageJ Analysis: Bessel beam



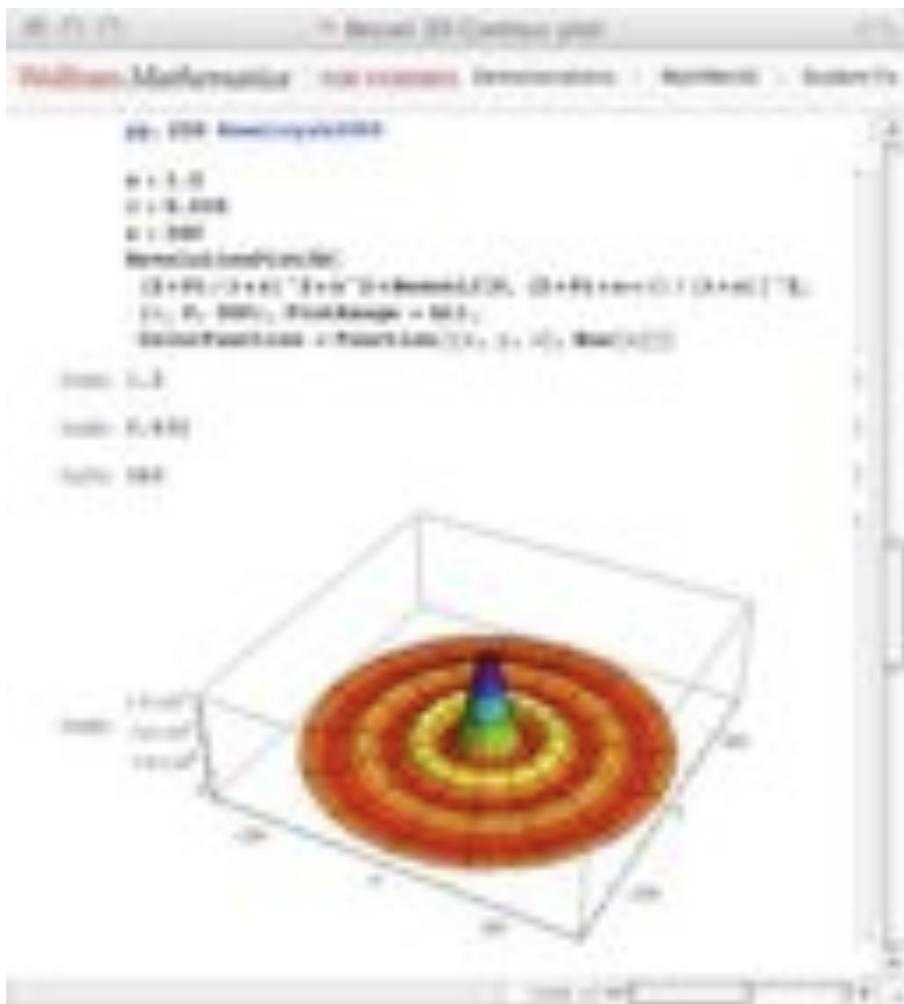
- Azimuthally averaged radial intensity profile of Bessel beam at a distance $Z = 340$ mm behind second Fourier lens
- Central spot size about $44.4 \mu\text{m}$

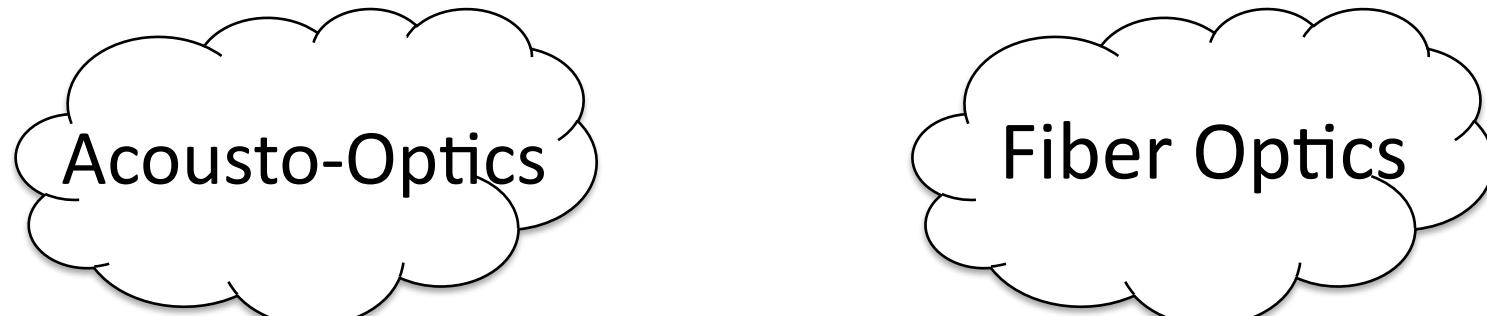


Modeling in Mathematica



- Currently creating theoretical model of the beam's intensity profile
 - Fit this model to the average intensity of the beam at a certain z distance
- Also graphing the z dependence of the theoretical and experimentally determined central spot size





Hundreds of papers later...

```
graph TD; A((Acousto-Optics)) --> C[Acoustic Vortices]; B((Fiber Optics)) --> C
```

Acoustic Vortices

Dashti 2006

TAG Lens

McLeod & Arnold 2008

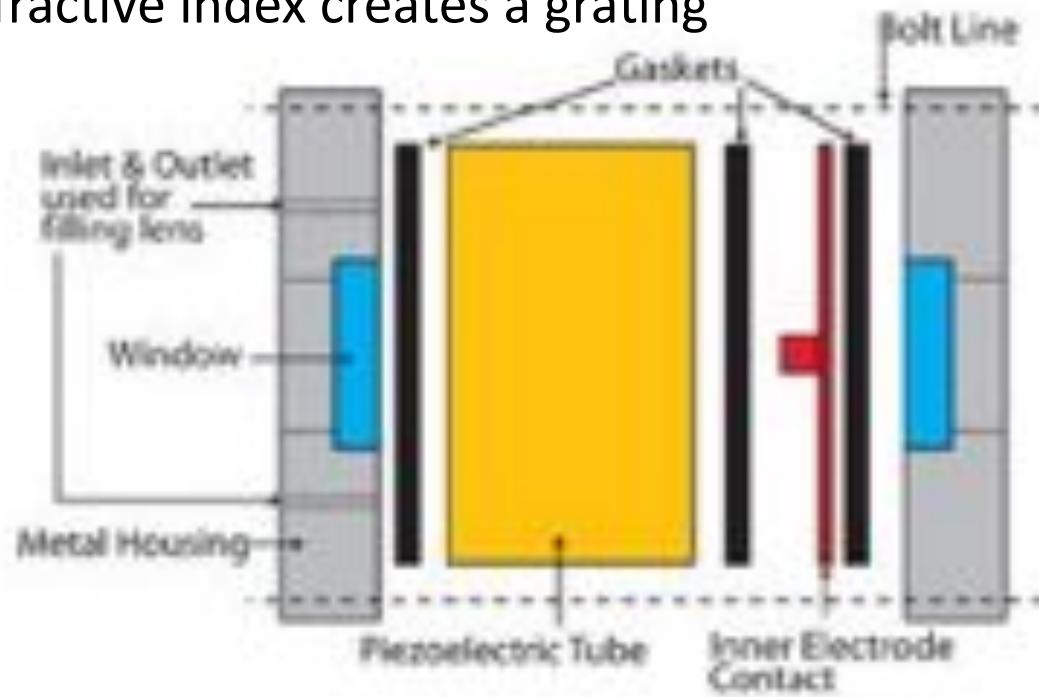
Bessel Beams

Melia

```
graph TD; C[Acoustic Vortices] --> D[TAG Lens]; D --> E((Bessel Beams)); E --> F((Melia))
```

Tunable Acoustic Gradient Index of Refraction Lens (TAG lens)

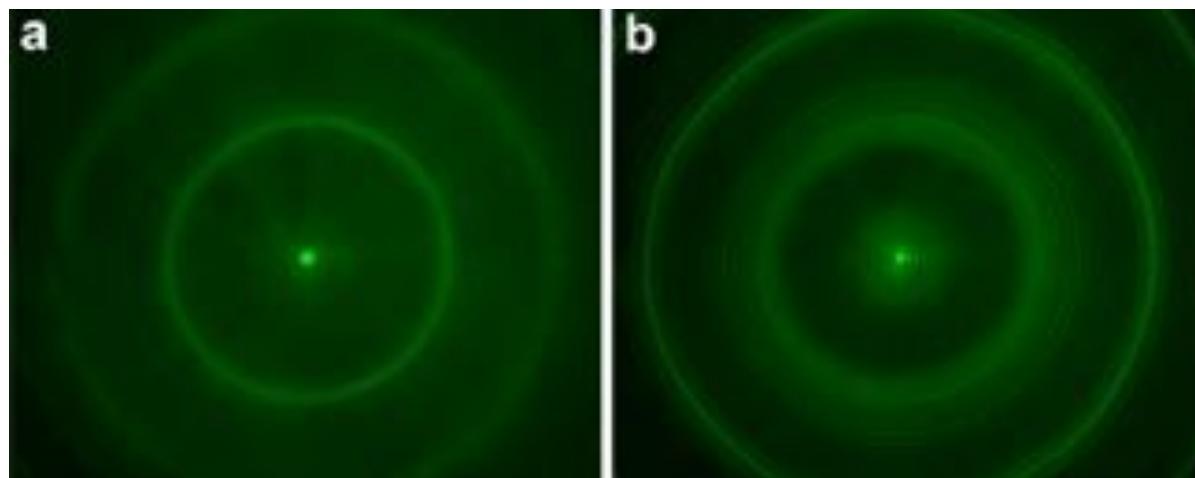
- A cylindrical cavity filled with a viscous fluid (silicone oil)
- A piezoelectric ring is driven to provide an radially symmetric acoustic wave
- Frequency range of 250-500 kHz at amplitudes from 0-100 V
- Change in refractive index creates a grating
- Tunability!



E. McLeod and C.B. Arnold (2008).

TAG Lens

- Invented by Craig Arnold, a professor at Princeton (2008 paper)
- Co-founded TAG Optics Inc. to commercialize
- Receive a device in several weeks
- Does not make higher-order Bessel beams

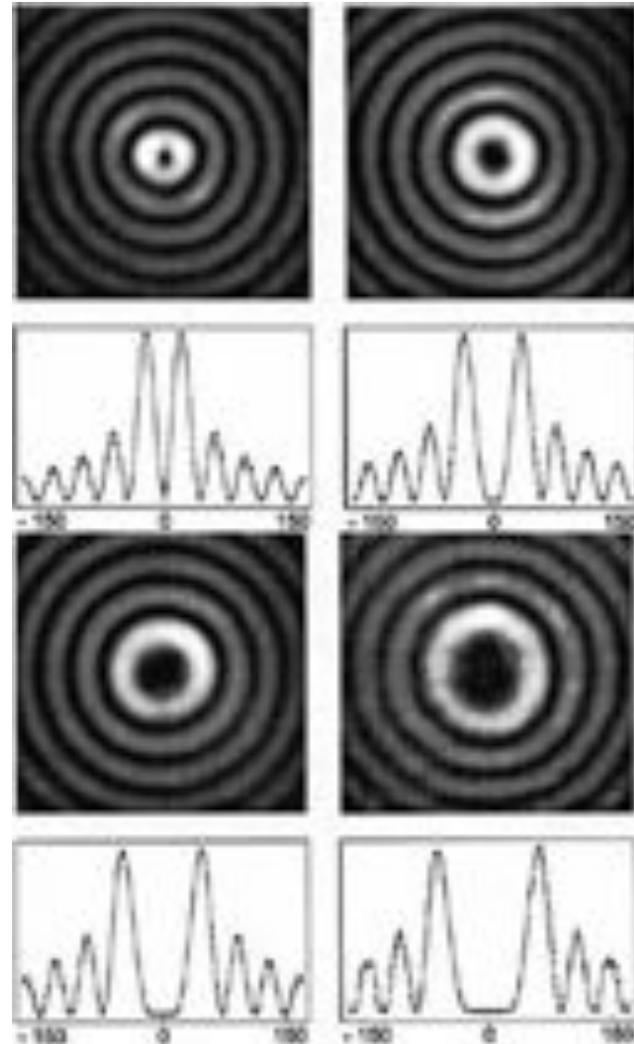


E. McLeod and C.B. Arnold (2008).

Azimuthal Phase Variation

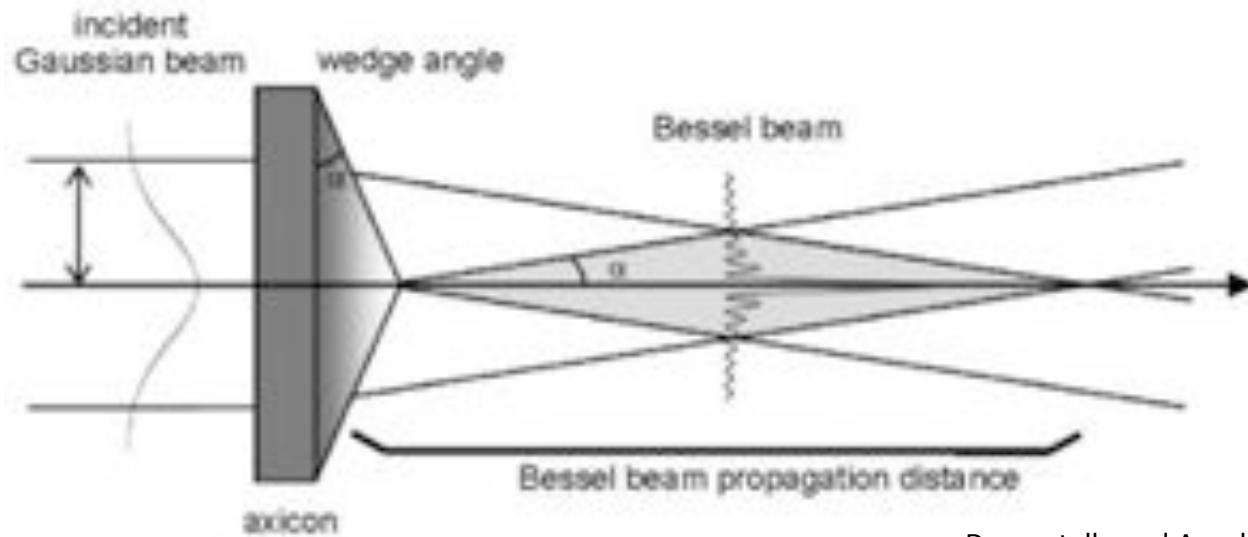
$$E_l(r, \phi, z) = A e^{i k_z z} J_l(k_r r) e^{i \phi l}$$

- Zero order ($l = 0$)
 - No phase variation
 - Bright central maximum
- Higher-order ($l > 0$)
 - Azimuthal phase variation
 - Dark central
- Conservation of topological charge
 - Laguerre-Gaussian (LG) beam with initial orbital angular momentum



Arlt and Dholakia (2000)

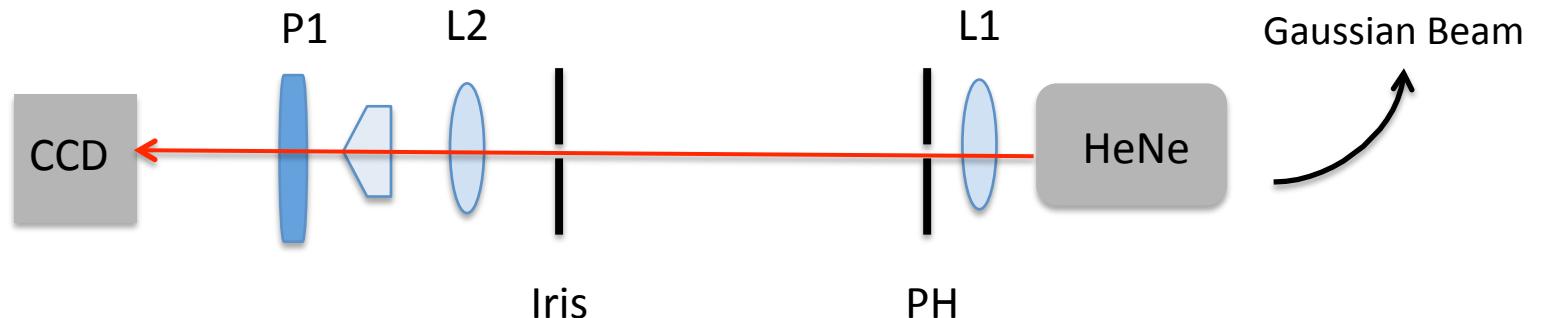
Axicon (Conical) Lens



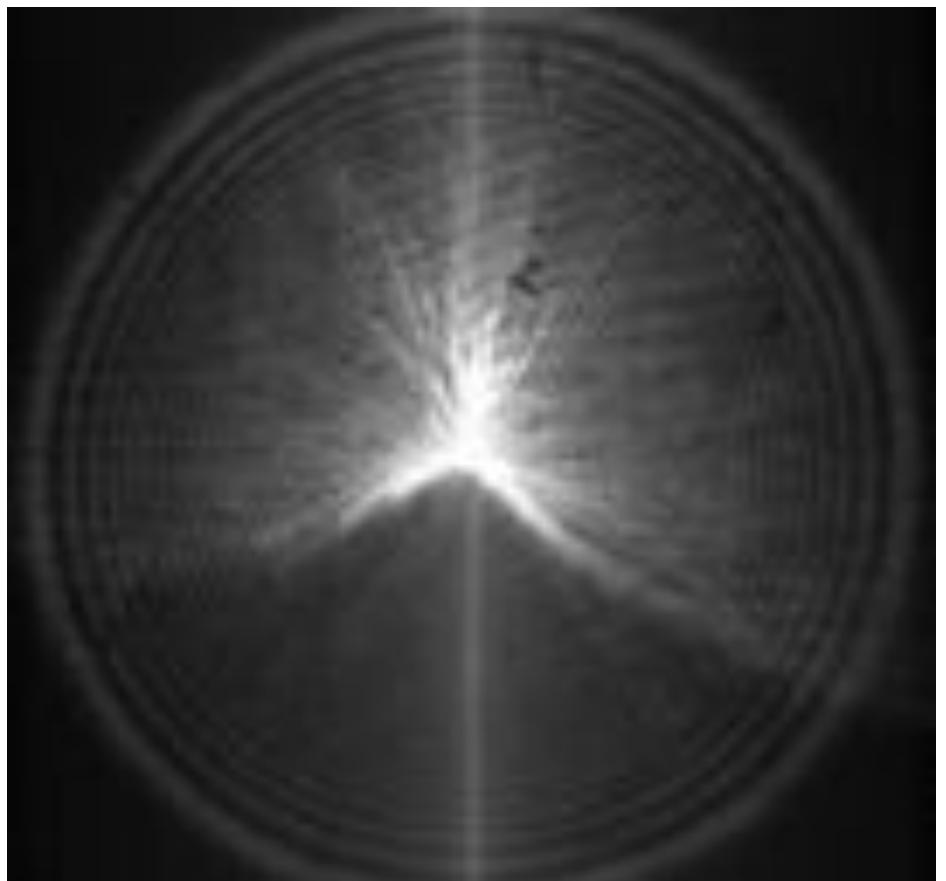
Duocastella and Arnold (2012)

- Conical lens with apex angle α and index of refraction n
- Bessel beam length proportional to incident beam diameter
- Most efficient method of creating Bessel beams

Zero- Order Setup

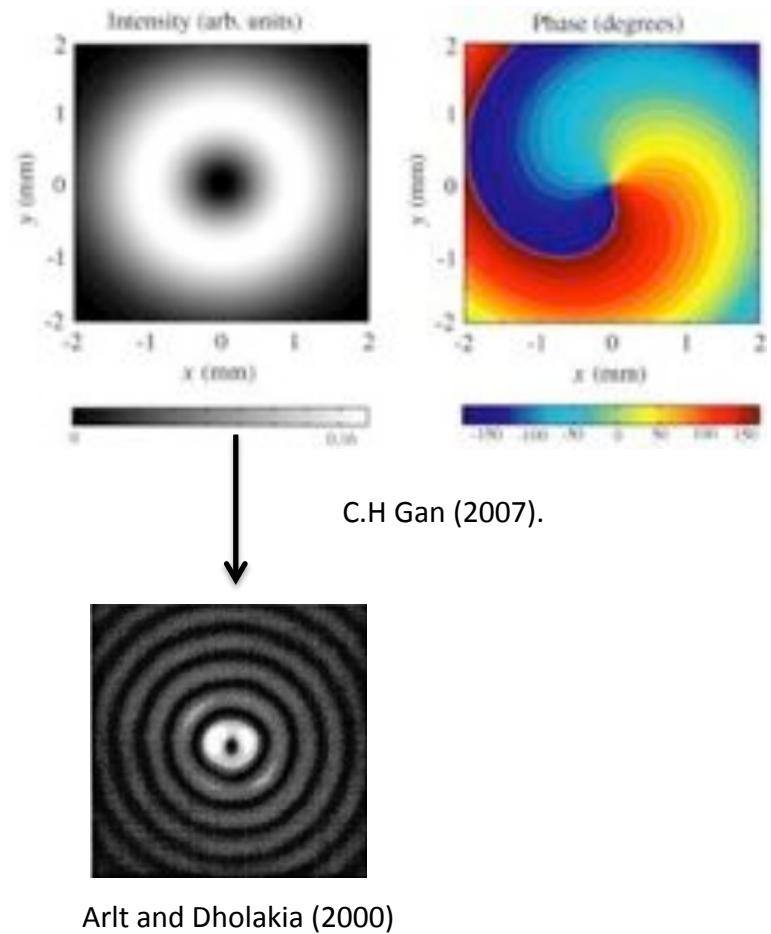


- Lens 1 and 75 micron pinhole
- Iris diaphragm and lens 2
→ Cleans up Airy pattern and collimates
- Polarizer
- Axicon (borrowed from CCNY)
→ 1° axicon angle & 25.44 mm diameter
→ $n \approx 1.55$
- CCD for recording



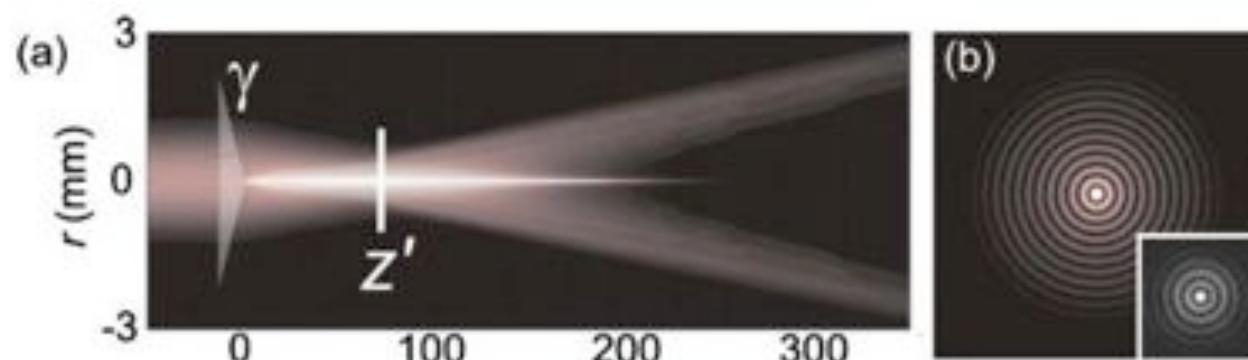
Higher-Order Setup

- Open Cavity HeNe Laser
- Astigmatic Mode Converter
→ convert to LG beam
- Pair of Lenses (Telescope)
→ $f = 35 \text{ mm}$ & 750 mm
- Axicon lens



Conclusion

- Bessel beams have interesting properties and important applications
- There are a variety of ways to make them
- This was a good topic for a teaching laboratory!



Milne (2008)

Acknowledgements

Founder of the Laser Teaching Center

- Hal Metcalf



Mentors

- John Noé
- Marty Cohen



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and the Laser Teaching Center at Stony Brook University

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