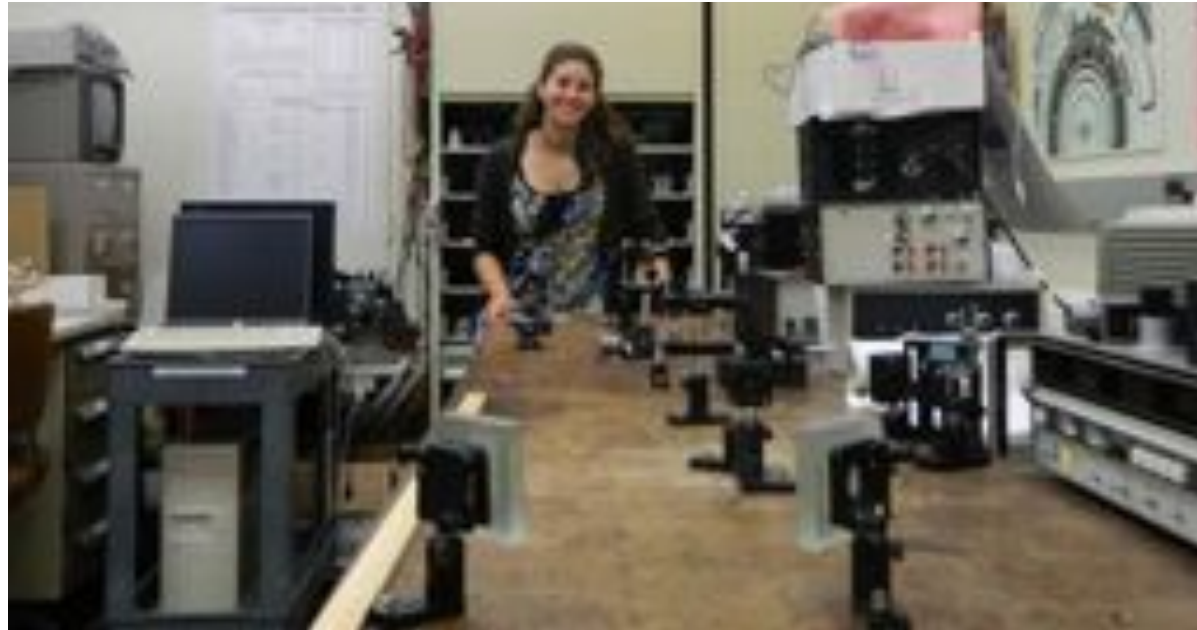


Creating Bessel Beams with a 4-f Spatial Filter



Melia Bonomo, Dickinson College '13
John Noé and Marty Cohen

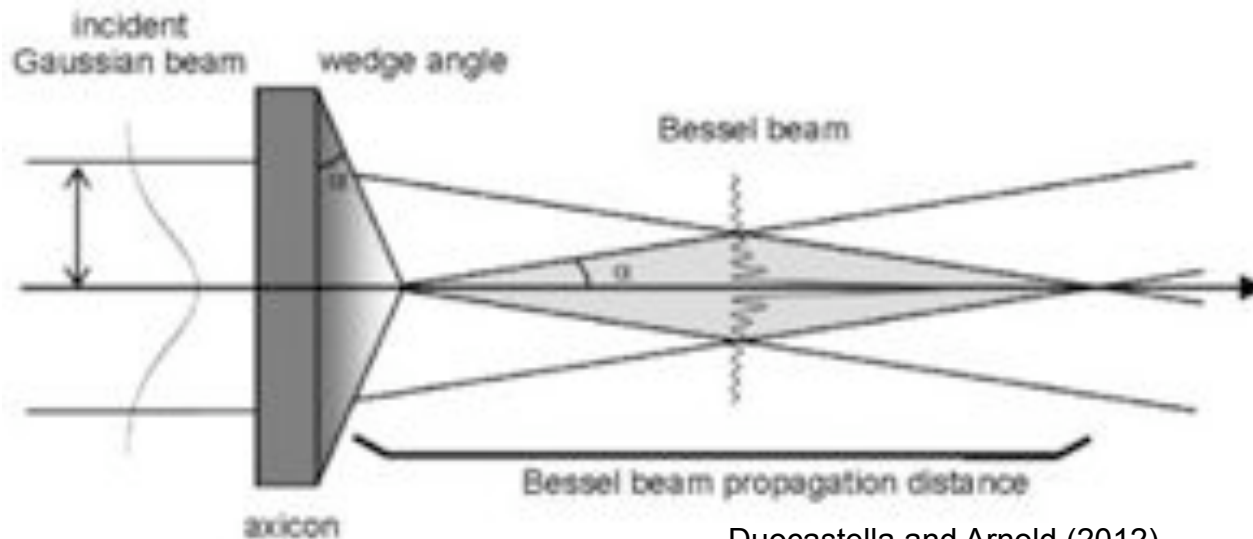


Stony Brook University
Laser Teaching Center
Summer 2012



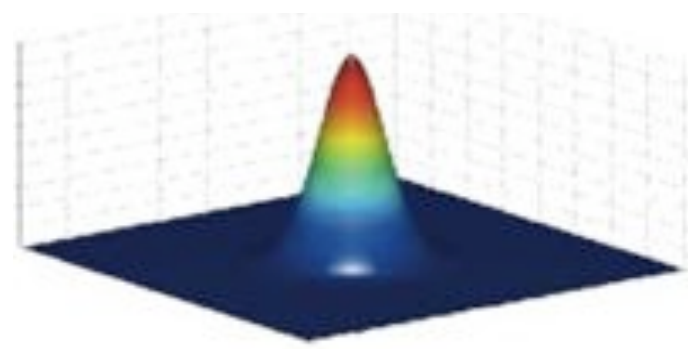
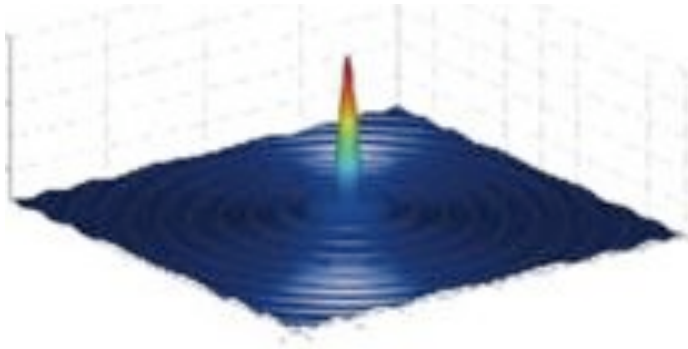
Overview

- Bessel beam properties
- Generating Bessel beams
 - (Axicon, 1953 McLeod)
 - Annular Aperture, 1987 Durnin, Eberly
 - 4-f Spatial Filter, 2009 Kowalczyk
- Imaging and analyzing the beam

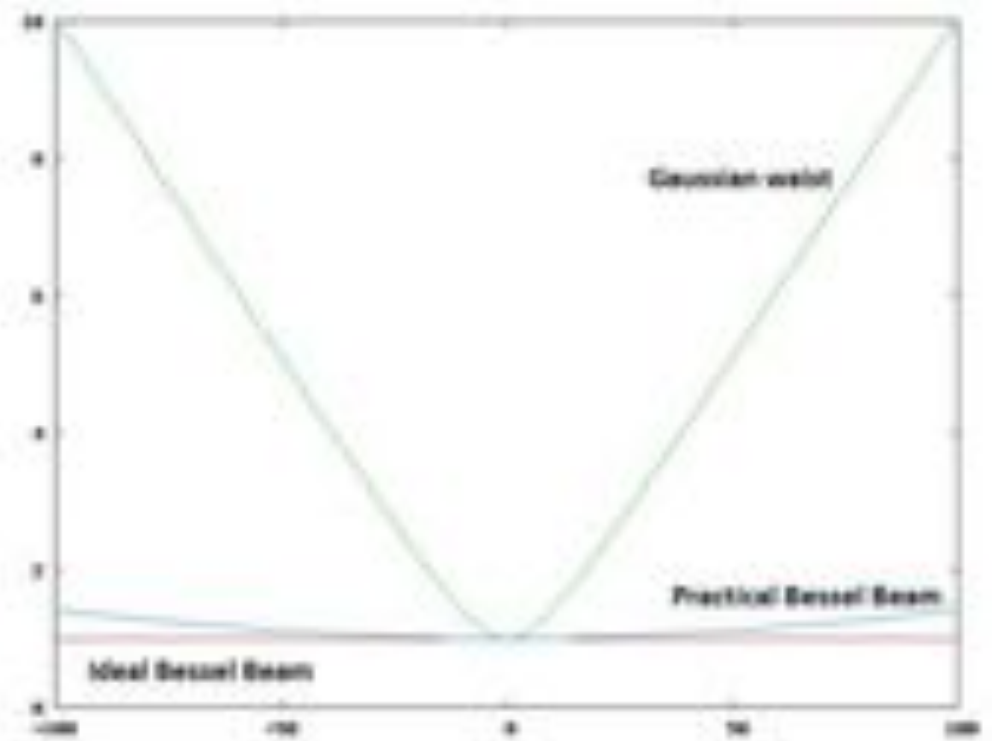


Duocastella and Arnold (2012)

Bessel vs. Gaussian Beams

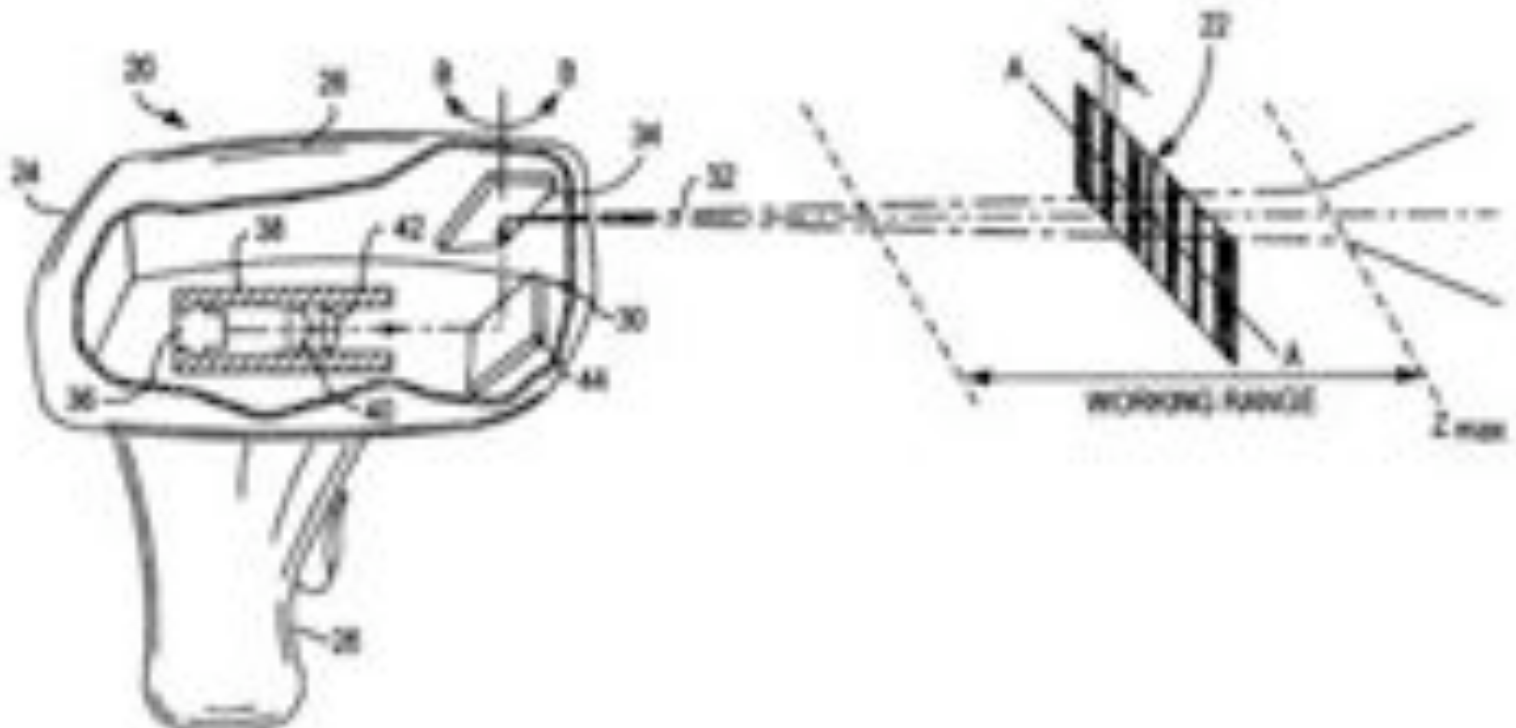


- Non-diffracting
- Thin, infinitely long core with concentric rings
- Ideal Bessel beams cannot be experimentally created
- Close approximations are possible



Most Widespread Application

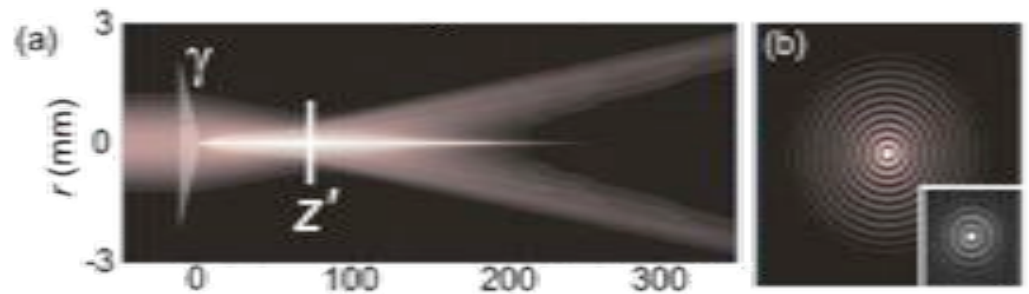
- Employing a Bessel beam greatly increases the working range of a barcode scanner



Gurevich 2003

Geometry and Math

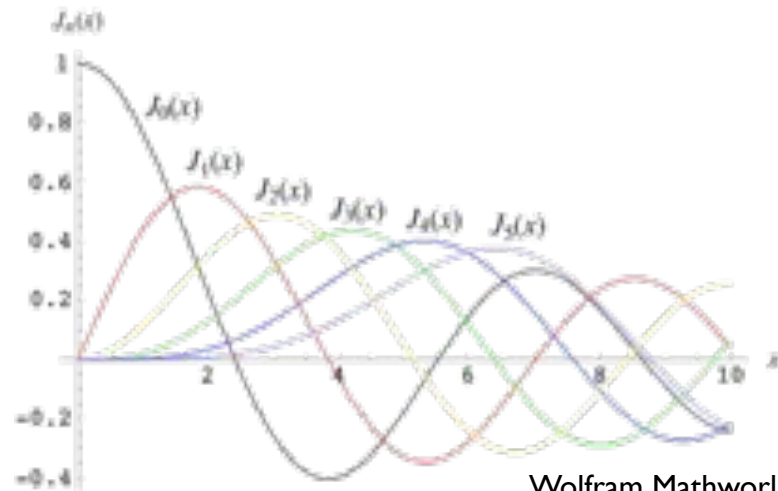
- Superposition of plane waves with k-vectors lying on surface of cone
 - Creates central max and plurality of side lobes



Milne (2008)

$$E_l(r, \phi, z) = A e^{i k_z z} J_l(k_r r) e^{i \phi l}$$

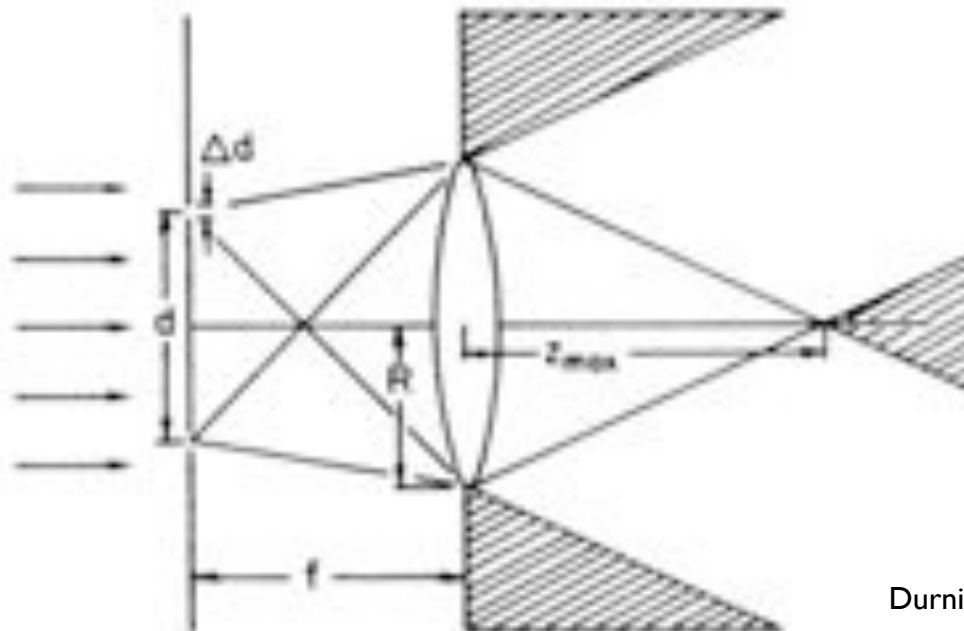
- Electric field amplitude proportional to Bessel function
- Zero-order or Higher-Order beams



Wolfram Mathworld, 2012⁵

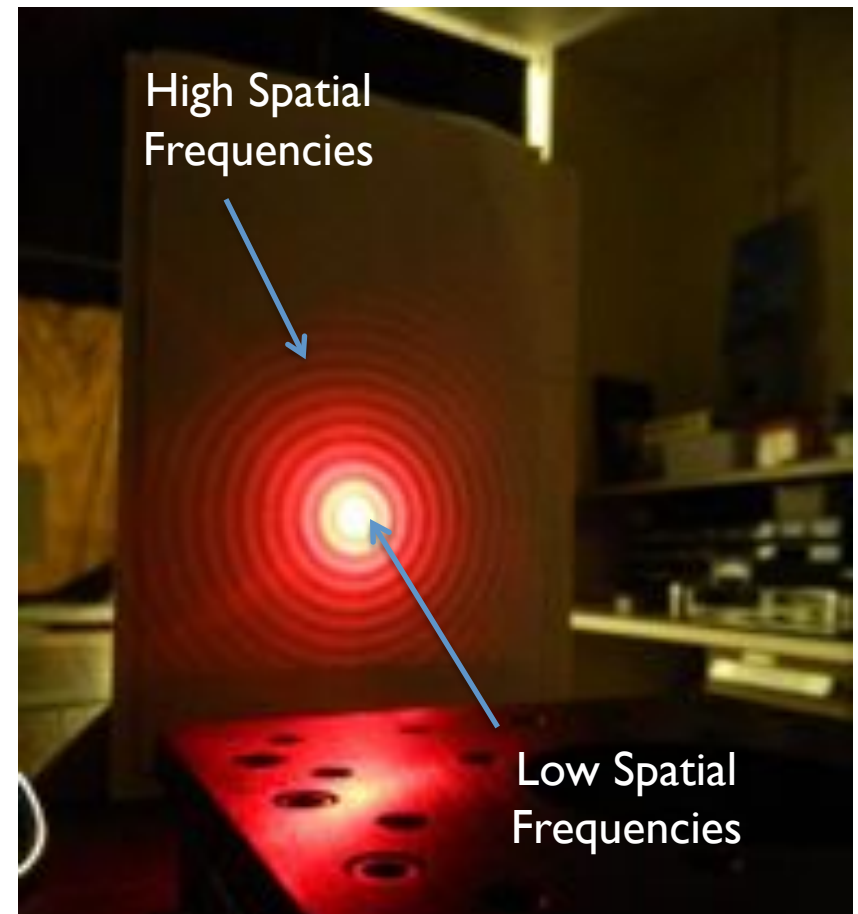
Creating Bessel beams with an Annular Aperture

- Fresnel diffraction of thin ring light source
- Durnin and Eberly 1987
 - 2.5 mm diameter, 10 micron wide
- Lens refocuses the diffracted ring of light to create conical superposition of plane waves

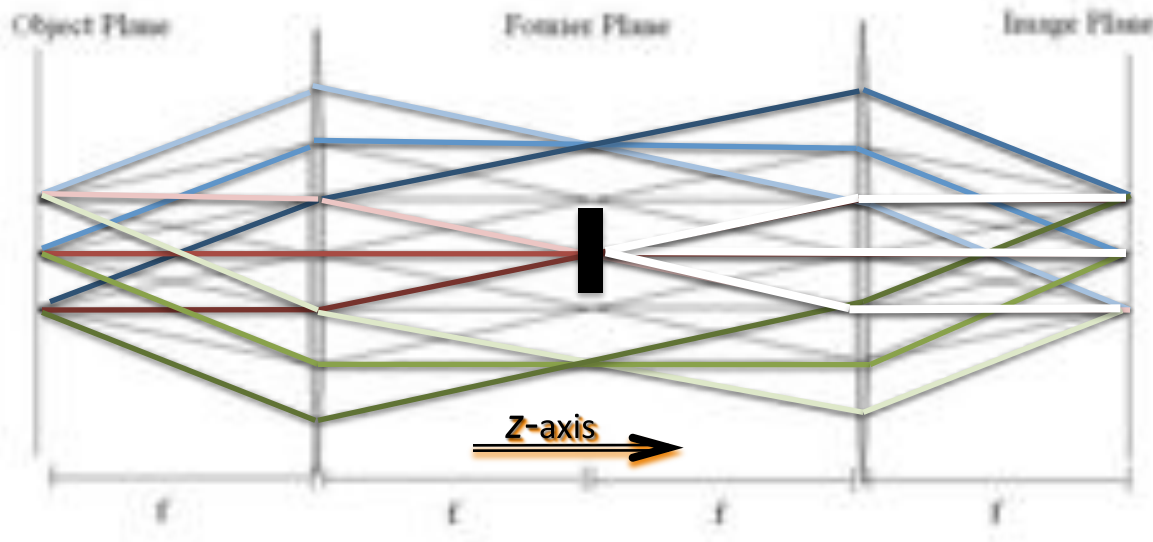


Creating a ring of light through spatially filtering a circular aperture

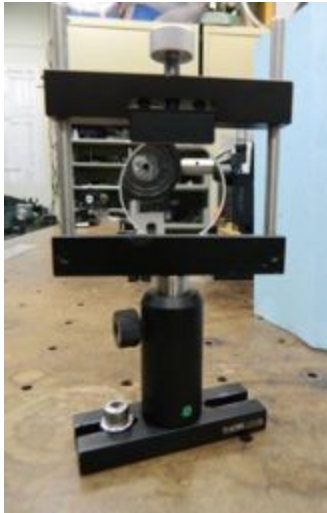
- Pinhole diffraction pattern in Fourier plane
- Fourier optics basics:
 - High spatial frequencies: object edges
 - Low spatial frequencies: overall quality
- Edge-enhanced image of the circular aperture



4-f Spatial Filtering Method



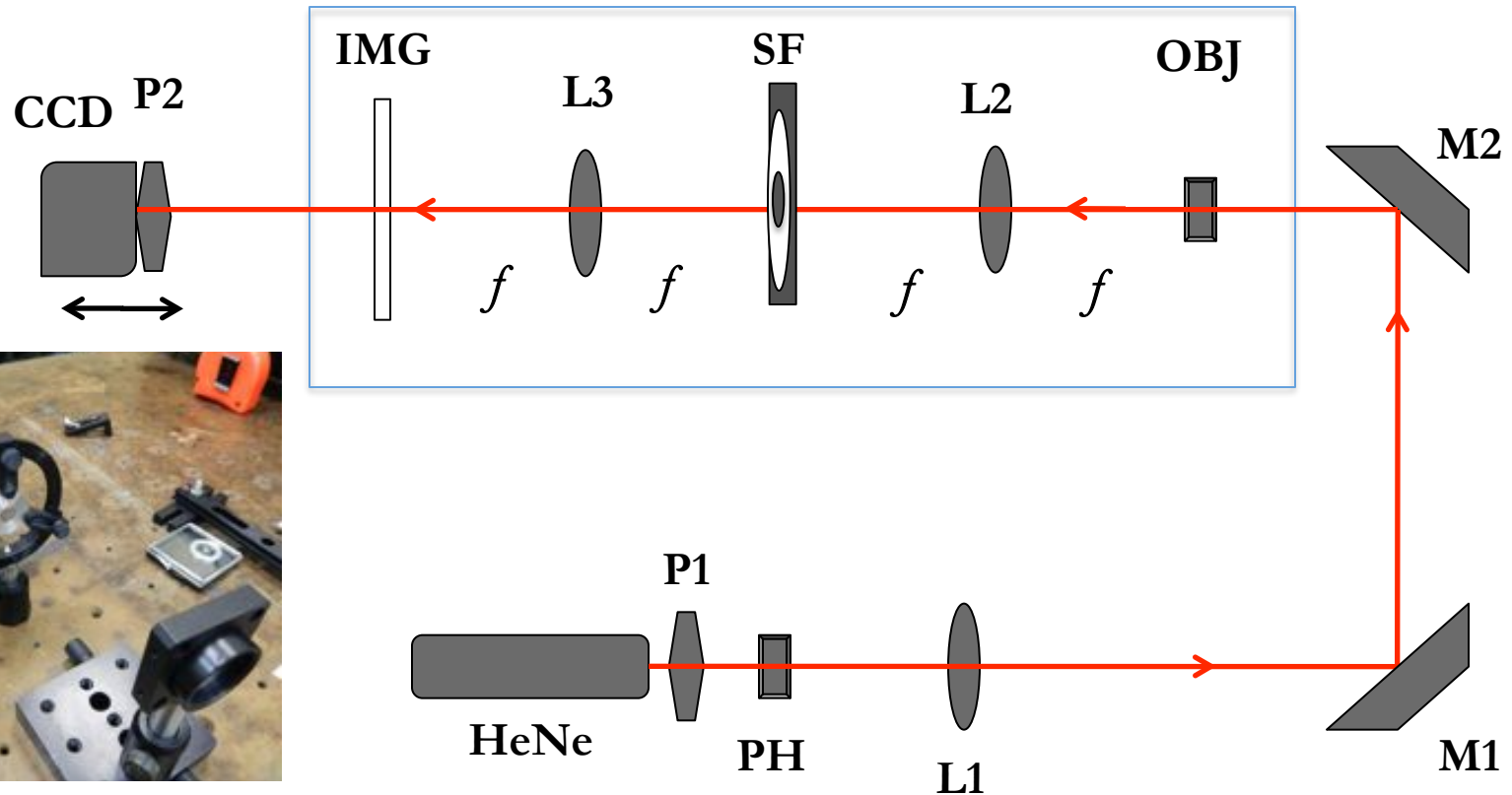
- Kowalczyk et al. (AJP, 2009)
- Lens organizes spatial frequencies of object
 - Rays bent at same angle are part of the same diffraction order of the pattern in the Fourier plane
- The diffraction pattern is the Fourier transform of the object
- Inverse image created in image plane



Setup Design

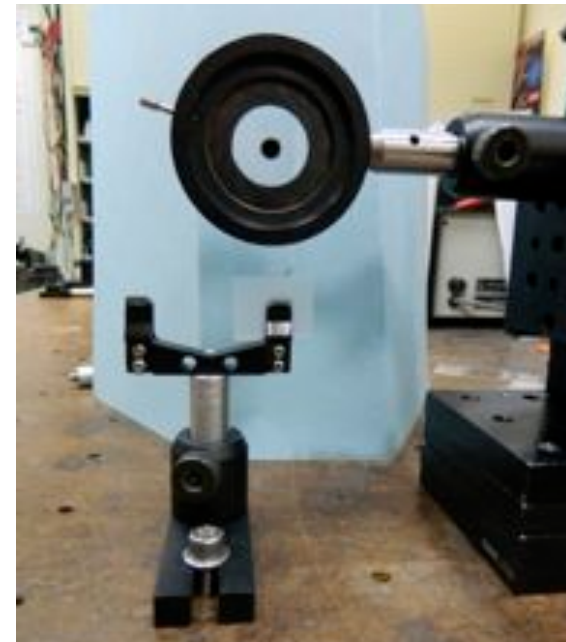
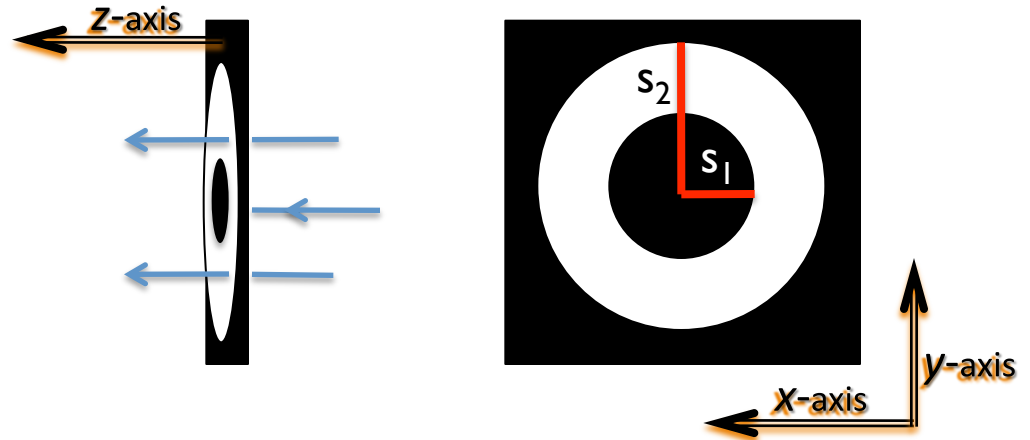


← Z-axis



The filter dimensions

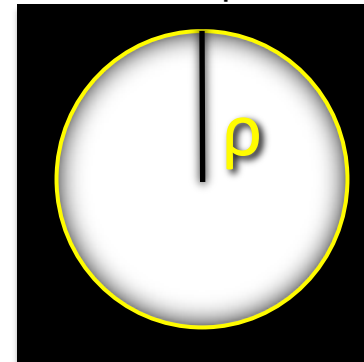
- Inner radius 3 mm
 - To block the low frequencies
- Outer iris diaphragm radius 10 mm
 - Limits the high frequencies coming through too
- Why is there a limit on the outer dimension?



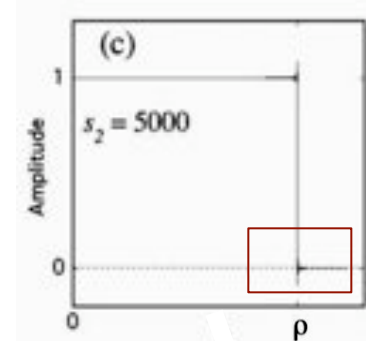
Gibb's phenomenon

- Always a zero in the middle of the diffracted field at $r = \rho$
- Causes double-lobed amplitude at edge of aperture

circular aperture

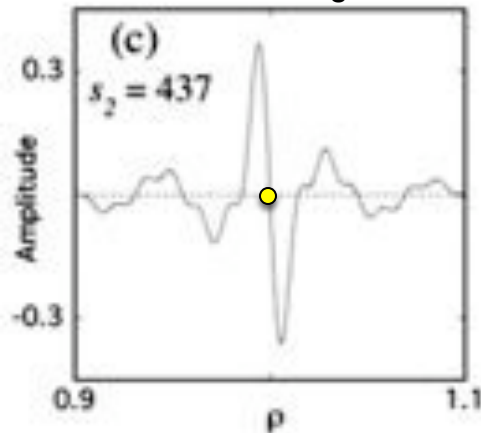


amplitude at edge of aperture

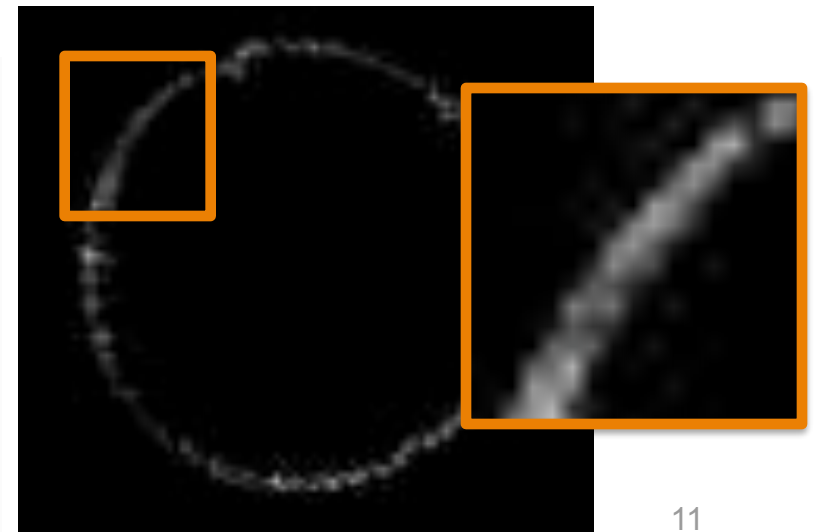
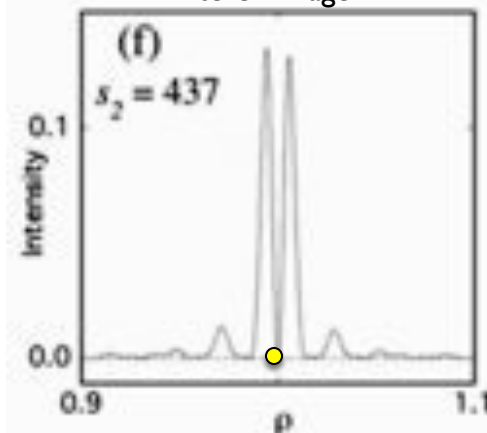


This is the difference between our ring and one that would come from a uniformly illuminated annular slit!

amplitude at edge of filtered image

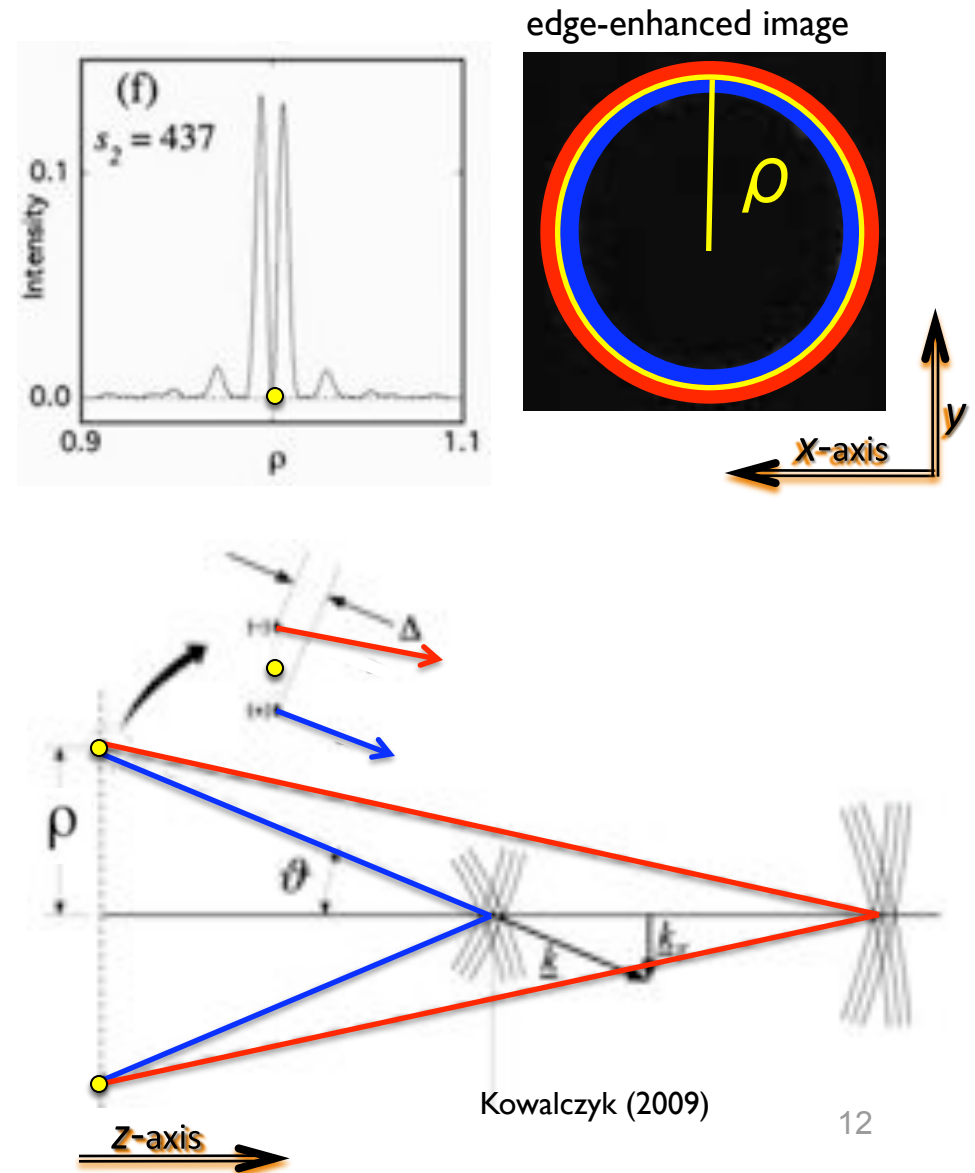


intensity at edge of filtered image



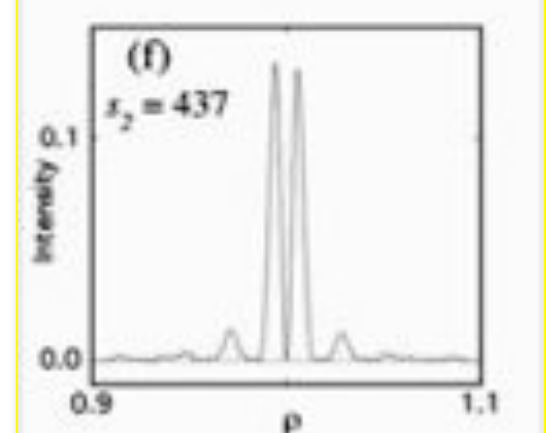
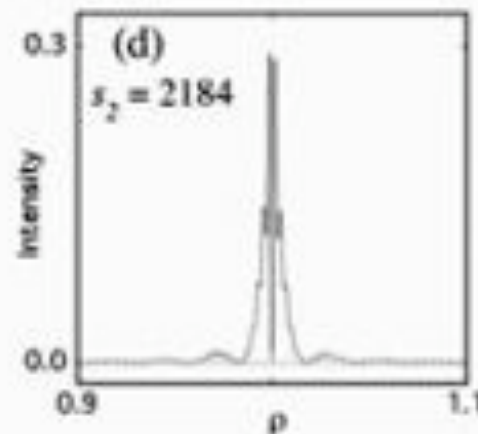
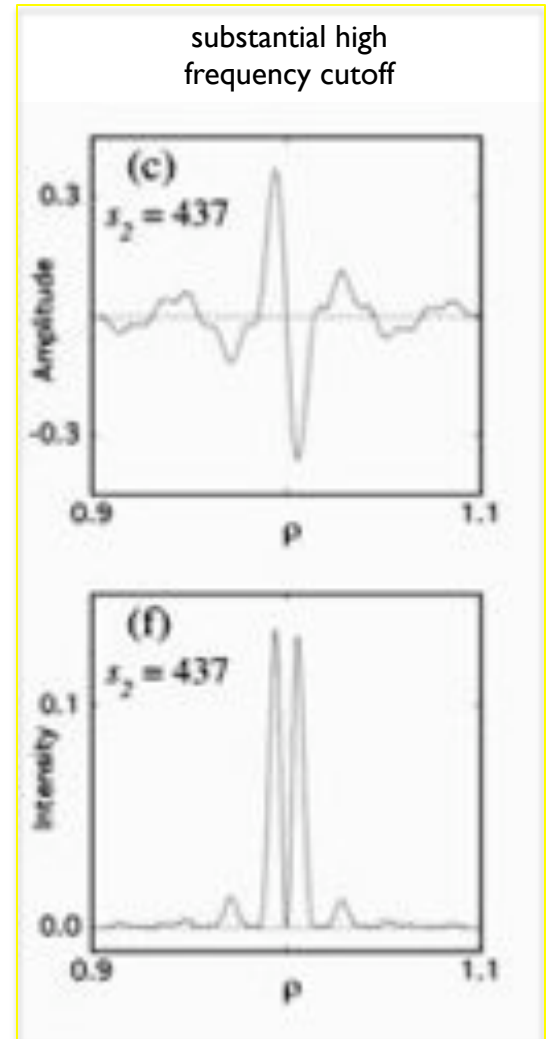
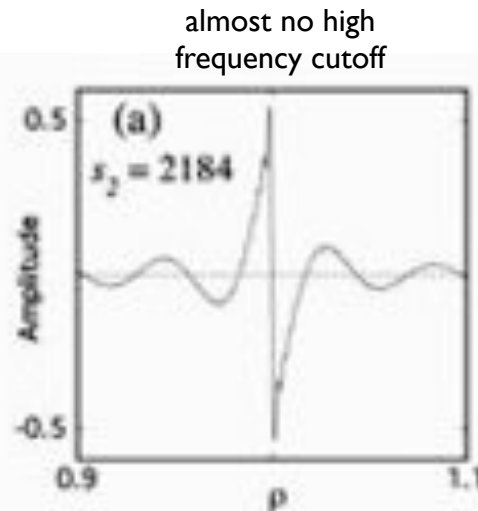
Forming the Bessel beam

- Propagation delay Δ between double-lobed intensity
- As you go farther on z-axis the lobes spread apart
 - constructive interference
 - start of Bessel beam
- Until a certain point where the lobes are too spread
 - destructive interference
 - end of the Bessel beam



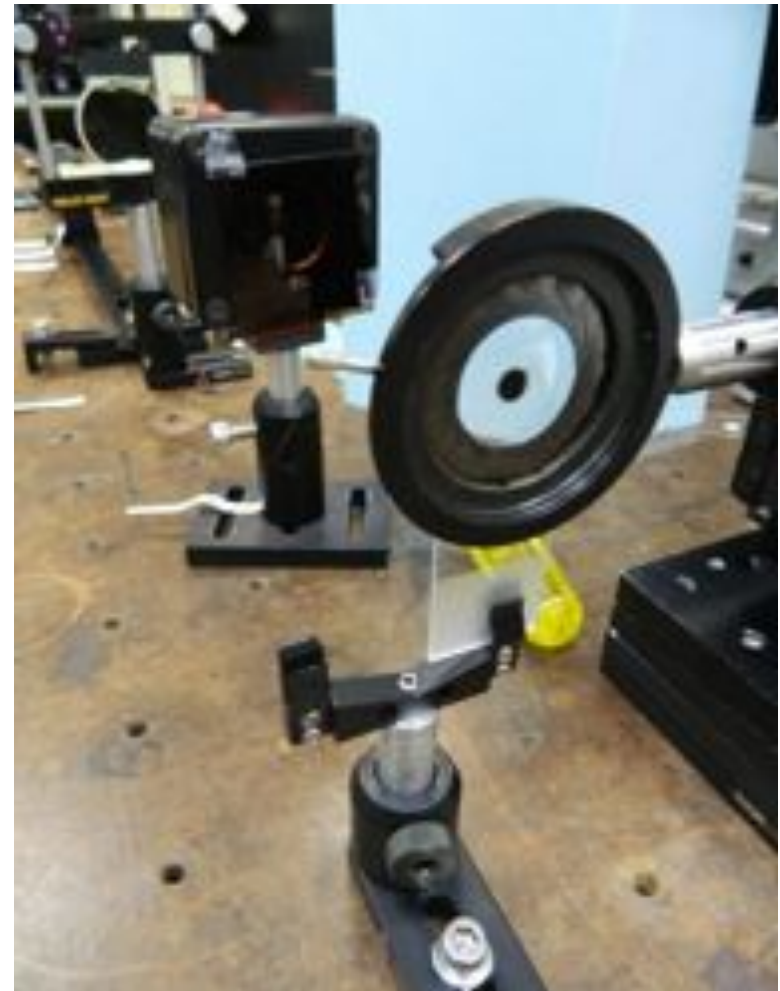
Effect of outer frequency cutoff on separation between intensity lobes

- Cutting off high frequencies:
 - less of an overshoot
 - lobes are more distinguishable from each other
 - larger propagation delay between lobes
 - larger region of constructive interference on axis
 - longer Bessel beam

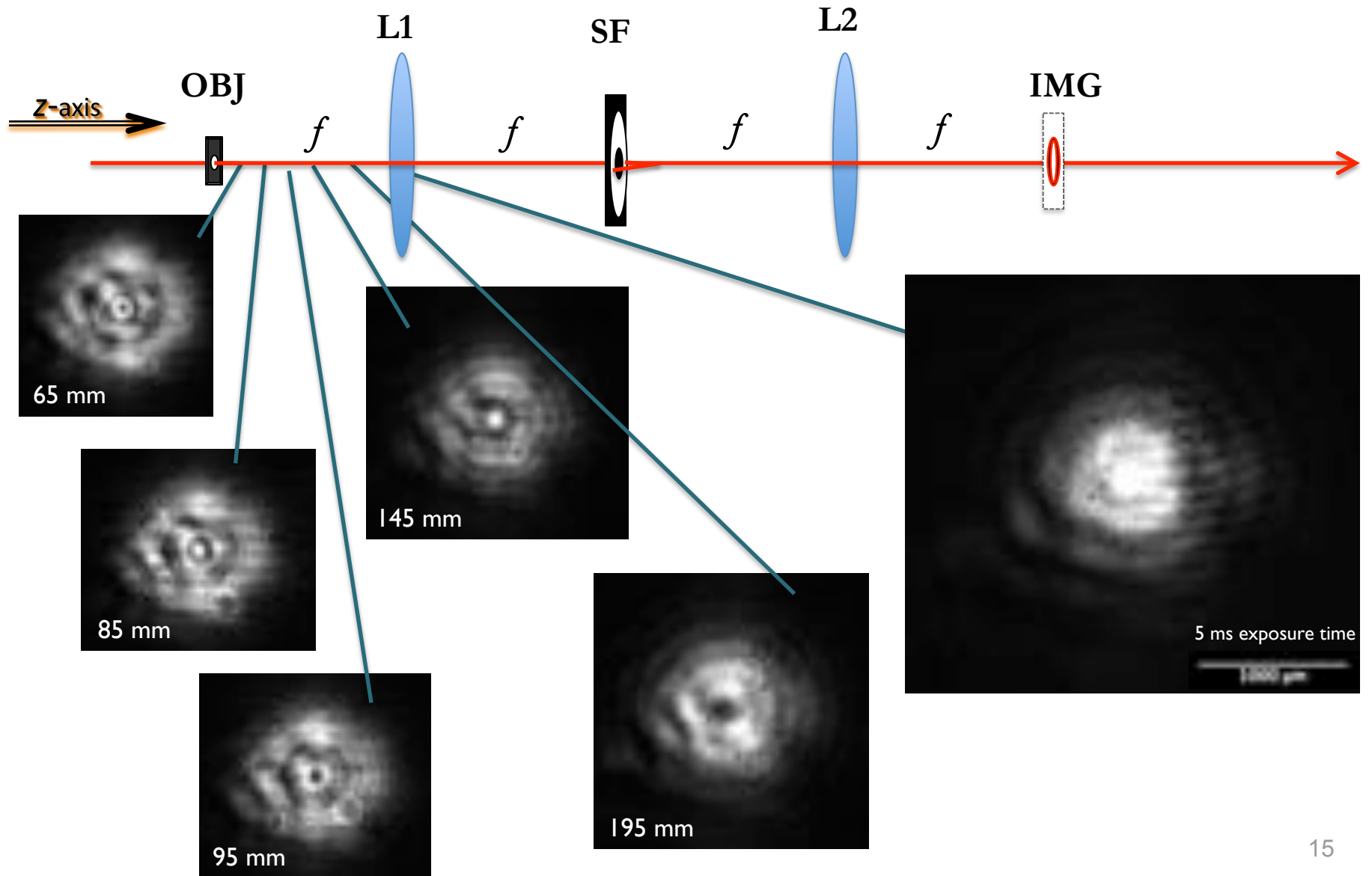


Electrim EDC 1000N images

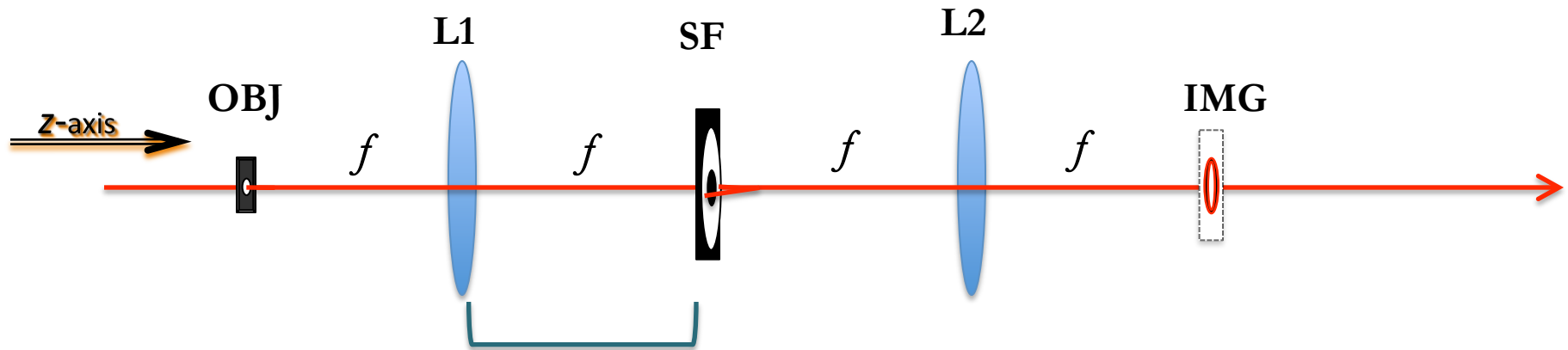
- 7.4 micron square pixels
- Polarizers to prevent saturation
- Recorded the evolution of the light field from the initial aperture to the final Bessel beam
- Images are transverse taken in transverse plane



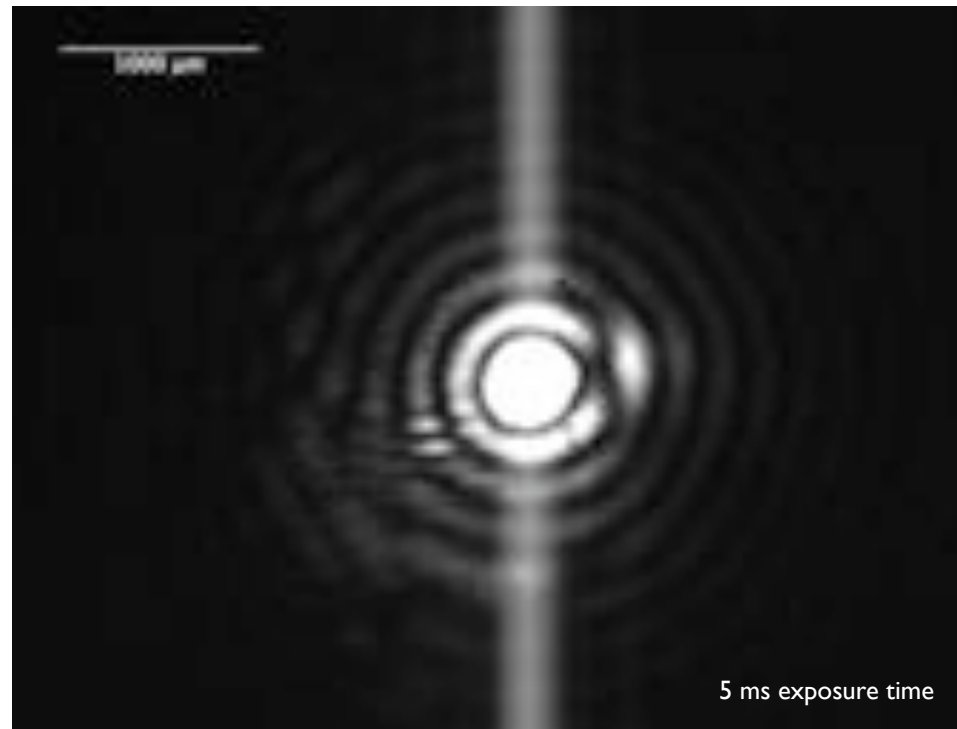
Object to Lens 1



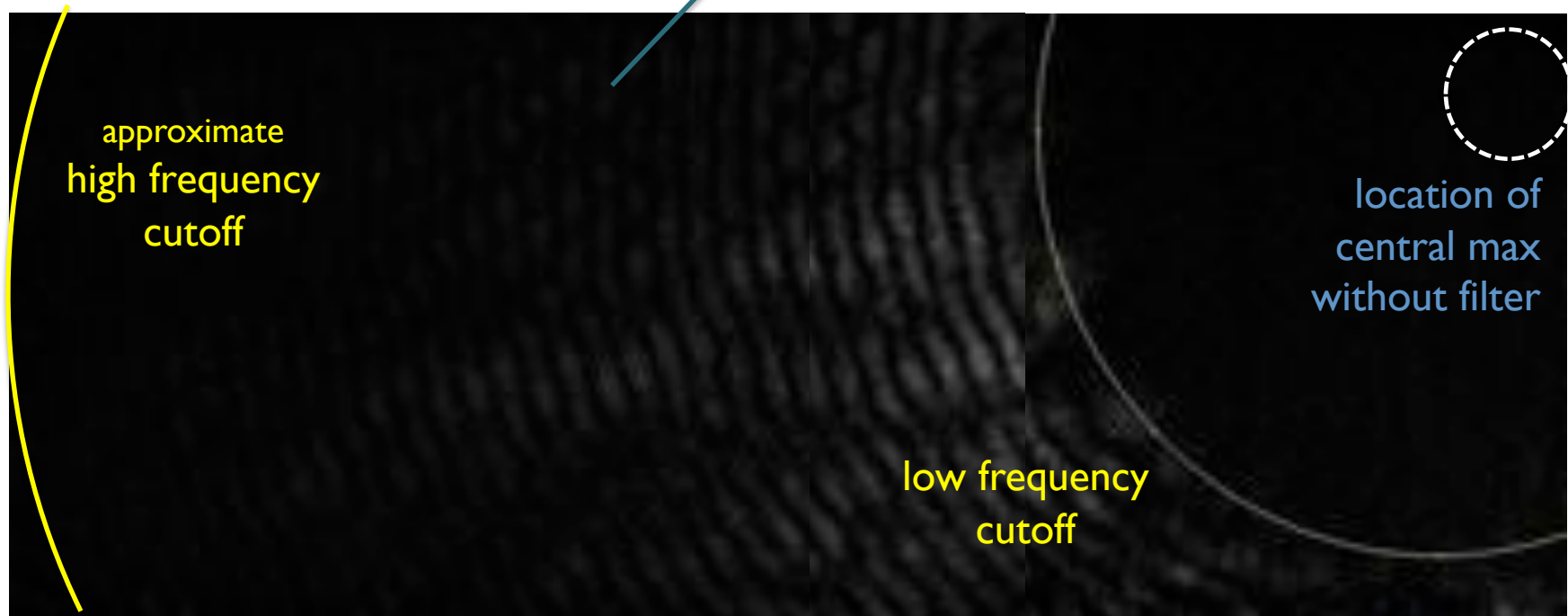
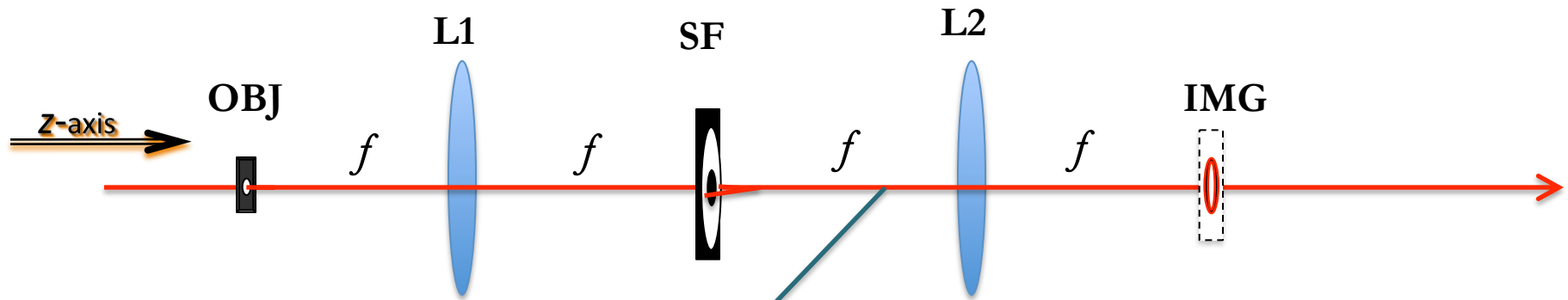
Lens 1 to Spatial Filter



classic Airy
pattern

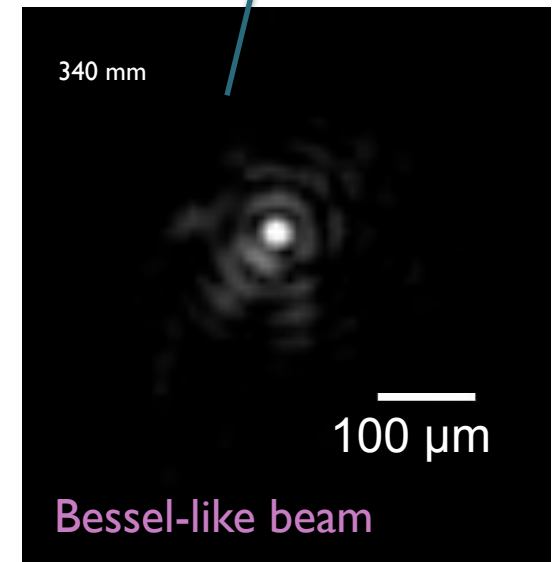
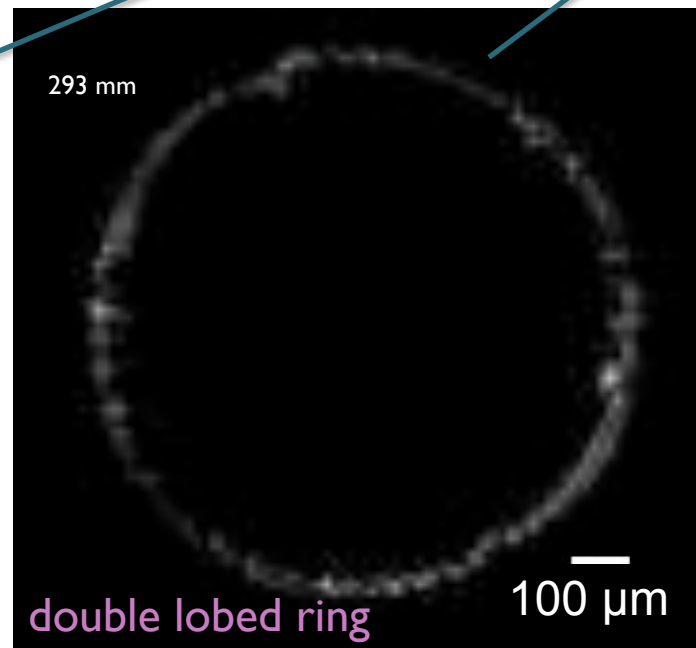
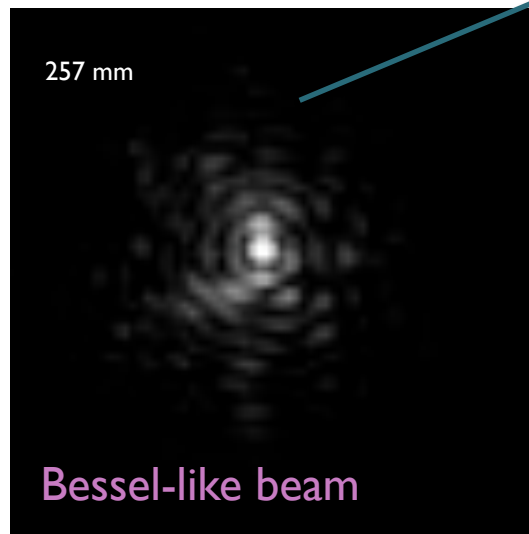
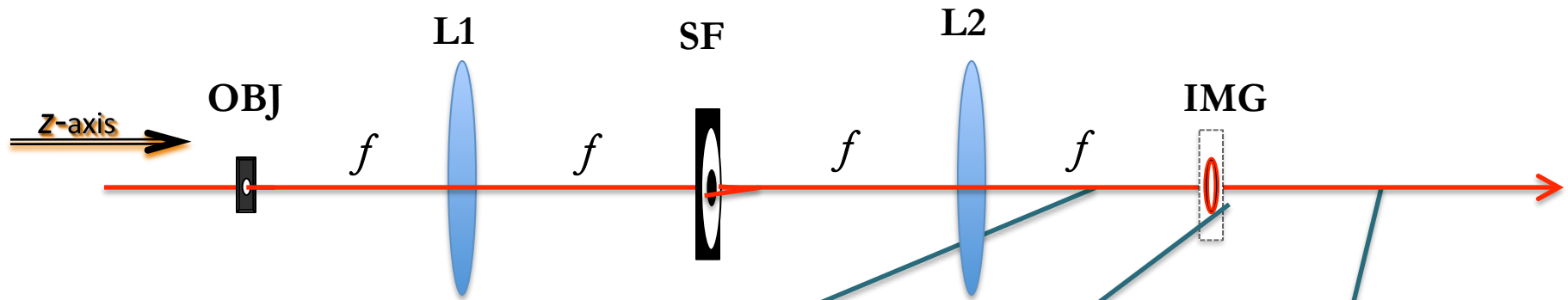


Spatial Filter to Lens 2



190 mm from Fourier plane

Lens 2 to Image Plane and Beyond



The formation of the Bessel beam

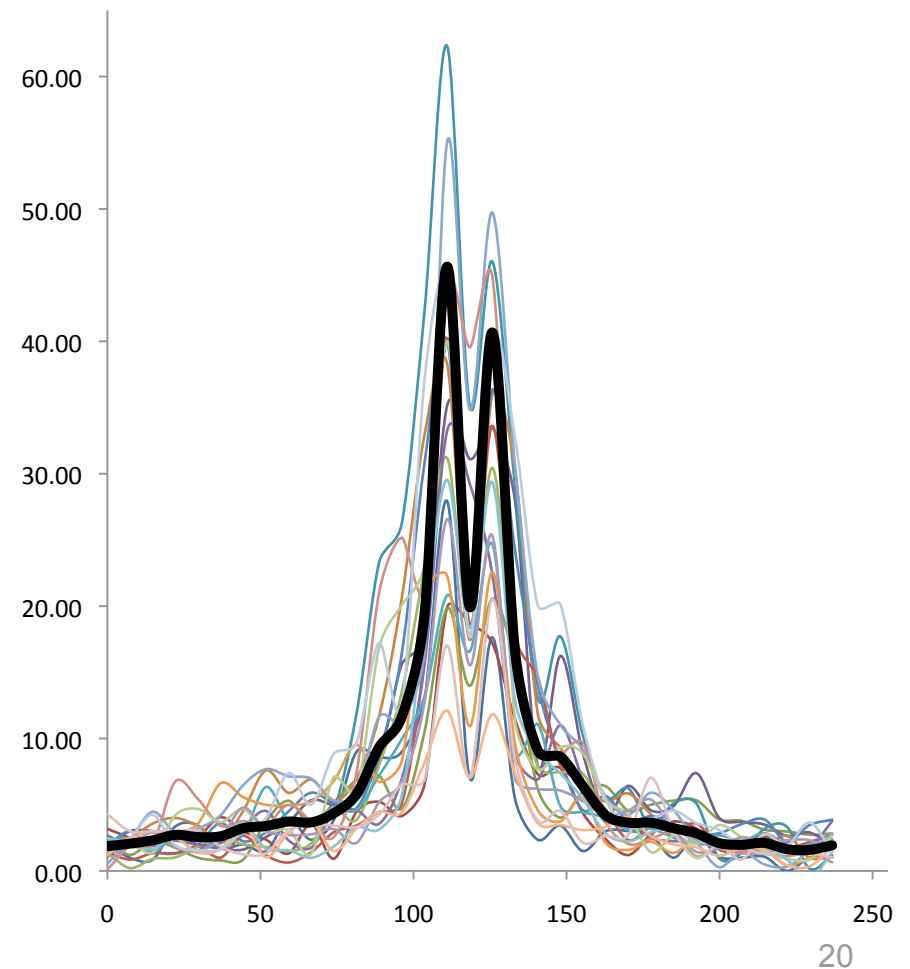
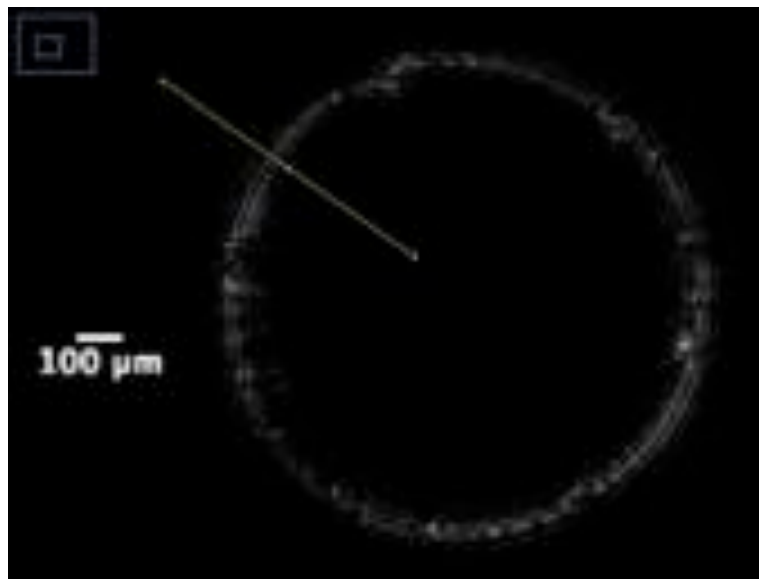


- Both Bessel beams (before and after the image plane) propagate for 47 mm with a core diameter under 45 microns
- Gaussian beam with an initial beam waist of 45 microns would double in area after 2.5 mm

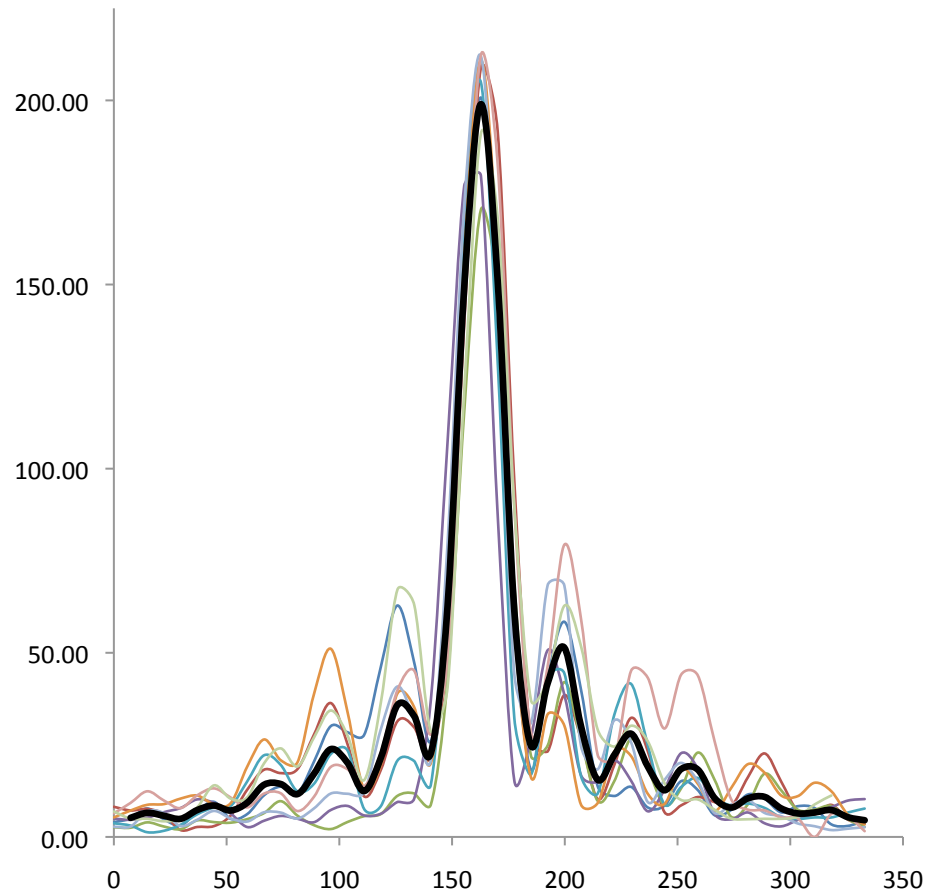
ImageJ Analysis: thin ring of light



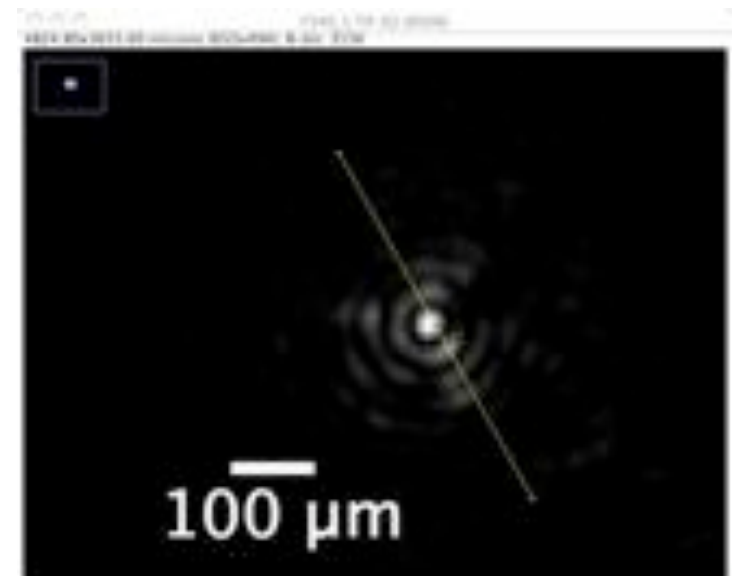
- Average radial intensity profile of double-lobed ring source at focal point
- Spacing between lobes about $14.8\text{ }\mu\text{m}$



ImageJ Analysis: Bessel beam



- Azimuthally averaged radial intensity profile of Bessel beam at a distance $Z = 340$ mm behind second Fourier lens
- Central spot size about $44.4 \mu\text{m}$



Conclusions

- We investigated an unusual way of creating Bessel beams.
- We studied the beam over a longer range than the original authors.
- This was a good topic for a teaching laboratory! It provided an introduction to Fourier optics and diffraction theory.

Key References

John M. McLeod, Optical Society of America **44** (8), 592 (1953).

J. Durnin, J. H. Eberly, and J. J. Miceli, Physical Review Letters **58** (15), 1499 (1987).

Jeremy M. D. Kowalczyk, Stefanie N. Smith, and Eric B. Szarmes, AJP 77 (3), 229 (2009).

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